

# INFRARED SYNCHROTRON RADIATION: FROM THE PRODUCTION TO THE USE

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The image shows a stylized profile of a human head in profile, facing right. Inside the head, there is a wavy pattern with a rainbow color gradient from yellow to green. Overlaid on this image are two email addresses in a black, serif font: "SISSI@Elettra" on the top line and "TeraFermi@Elettra" on the bottom line.



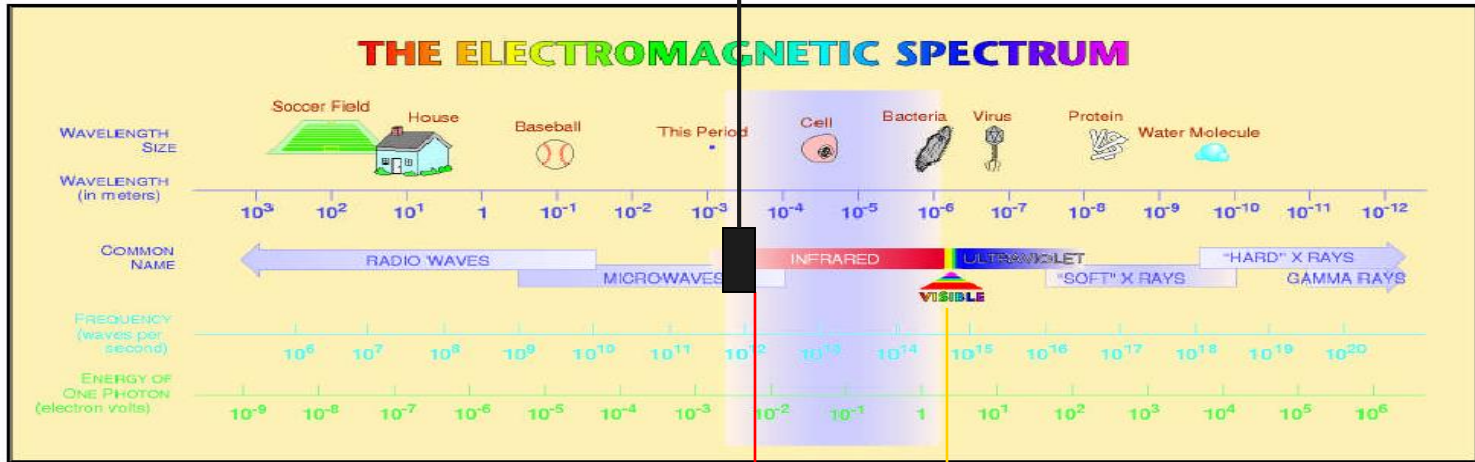
# Outline

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- Production and Properties of Infrared Synchrotron Radiation;
- Experimental Apparatus: Michelson Interferometry+Infrared Microscopy
- **Solid-State Applications:**
  - Superconducting Transition (THz and Far-IR Spectroscopy)
  - Gap determination
  - Spectral-Weight and penetration depth
  - Metal-to-Insulator Transitions
- **Biology:**
  - Cellular absorption and replication
- **Geological Applications:**
  - Microscopic fluid inclusions
- **Chemistry:**
  - Absorption at solid surfaces
- **New developments**
  - THz non linear Spectroscopy
  - Go beyond the diffraction limit: Infrared Nanoscopy

# Electromagnetic Spectrum

The “THz gap”, Collective Excitations in Macromolecules and exotic electronic materials



**IR Units:  $200 \text{ cm}^{-1} = 300 \text{ K} = 25 \text{ meV} = 50 \mu\text{m} = 7 \text{ THz}$**

FIR MIR NIR

Phonons;  
Drude absorption;  
Gaps in superconductors;  
Molecular Rotations;

Molecular Vibrations  
**Fingerprints** for  
Chemistry, Biology,  
And Geology

Molecular Overtones and  
Combinations bands;  
Excitons;  
Gaps in semiconductors

# Infrared History

*Volume 1.*

*July-August, 1893.*

*Number 1.*

THE  
PHYSICAL REVIEW.

A STUDY OF THE TRANSMISSION SPECTRA OF  
CERTAIN SUBSTANCES IN THE INFRA-RED.

BY ERNEST F. NICHOLS.

WITHIN a few years the study of obscure radiation has been greatly advanced by systematic inquiry into the laws of dispersion of the infra-red rays by Langley,<sup>1</sup> Rubens,<sup>2</sup> Rubens and Snow,<sup>3</sup> and others. Along with this advancement has come the more extended study of absorption in this region. The absorption of atmospheric gases has been studied by Langley<sup>1</sup> and by Ångström.<sup>4</sup> Ångström<sup>5</sup> has made a study of the absorption of certain vapors in relation to the absorption of the same substances in the liquid state, and the absorption of a number of liquids and solids has been investigated by Rubens.<sup>6</sup>

In the present investigation, the object of which was to extend this line of research, the substances studied were: plate glass, hard rubber, quartz, lamp-black, cobalt glass, alcohol, chlorophyll, water, oxyhæmoglobin, potassium alum, ammonium alum, and ammonium-iron alum.

<sup>1</sup> Report on Mt. Whitney Expedition, Profess. Papers, U. S. Signal Service, XV.

<sup>2</sup> Annalen der Physik und Chemie, N. F. XLV., p. 238.

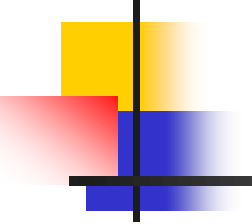
<sup>3</sup> Annalen der Physik und Chemie, N. F. XLVI., p. 529.

<sup>4</sup> Bihang till K. Svenska Vet.-Akad. Handlingar, Band 15, Afd. 1, No. 9.

<sup>5</sup> Öfversigt af Kongl. Vetenskaps-Academiens Forhandlingar, 1890, No. 7, Stockholm.

<sup>6</sup> Annalen der Physik und Chemie, N. F. XLV., p. 258.

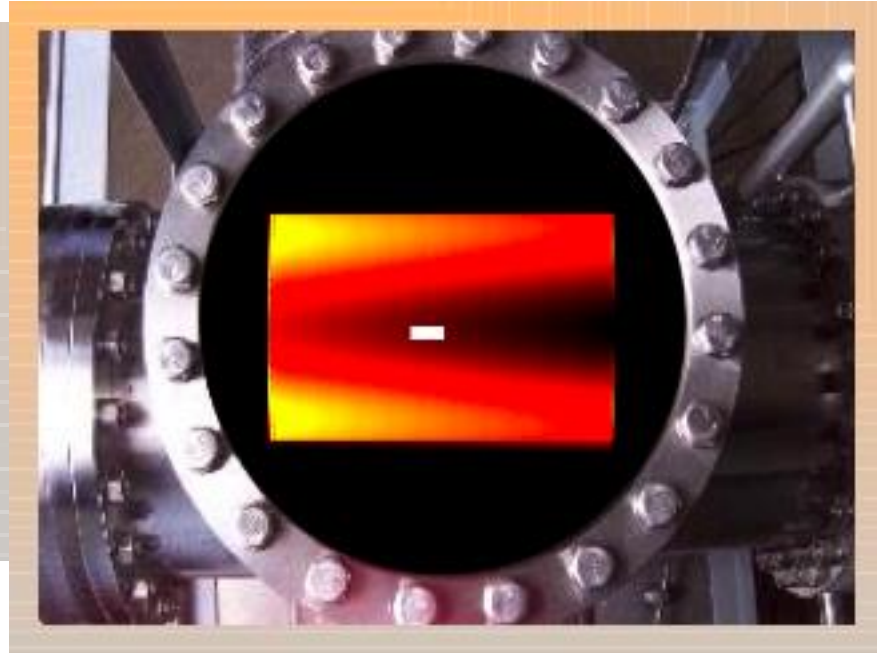
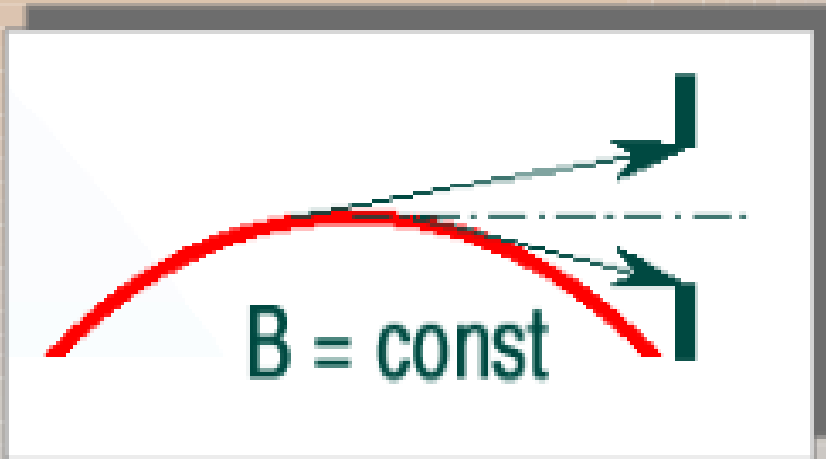
# ~ 50 IRSR Beamlines in the World

- 
- 1976 Meyer and Lagarde (LURE, Orsay) publish the first paper on IRSR
- 1981 Duncan and Yarwood observe at Daresbury the first IRSR emission
- 1985 The first IRSR spectrum (on N<sub>2</sub>O) is collected at Bessy (Berlin)
- 1986 The first beamline becomes operating at UVSOR (Japan)
- 1987 Beamline at Brookhaven (USA)
- 1992-94 Beamlines at Orsay (France), Lund (Sweden), Daresbury (GB)
- 1995 First international workshop on IRSR, Rome (Italy)
- 2001 First IR beamline in Italy (SINBAD@DAΦNE)
- 2006 Second beamline in Italy (SISSI@Elettra)
- 2015 First THz beamline in Italy (TERASPARC@SPARC)
- 2017 Second THz beamline in Italy (TERAFERMI@Elettra)

# Production of IRSR

## Standard Bending radiation

(emitted during the circular trajectory in the bending due to the constant B field)



$$P(\lambda) = 4.4 \cdot 10^{14} \times I \times \Theta_H \times bw \times (\rho/\lambda)^{1/3} \text{ photons s}^{-1}$$

$I$  is the current in amperes,

$\Theta_H$  (rads) the horizontal collection angle,

$bw$  the bandwidth in per cent,  $\lambda$  the wavelength, and  $\rho$  the radius of the bending

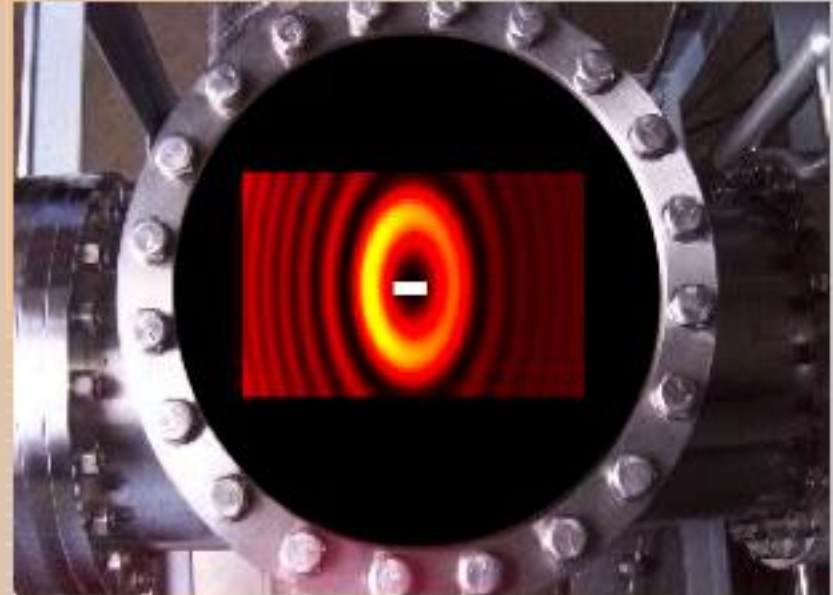
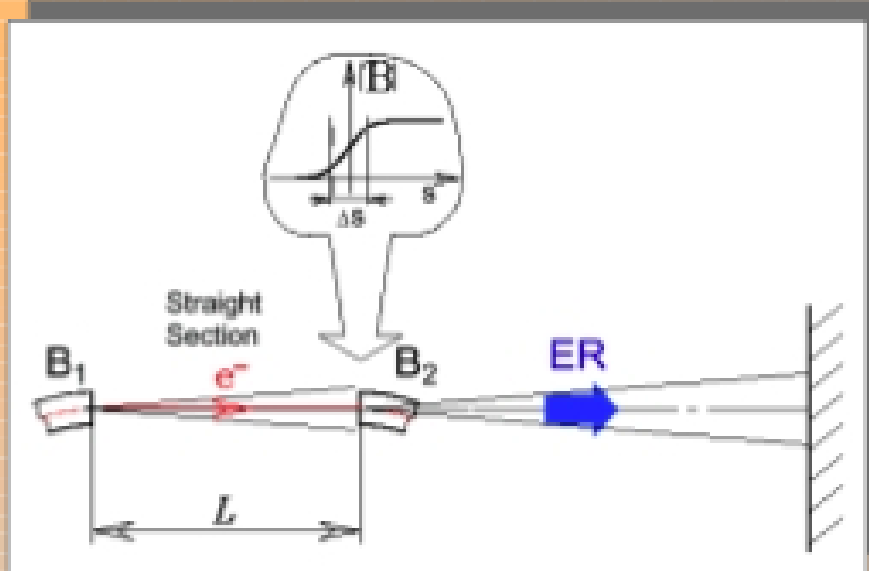
$$\Phi_{V-NAT}(\text{mrad}) = 1.66(1000 \times \lambda (\mu\text{m}) / \rho(\text{m}))^{1/3}$$

at ALS for  $\lambda = 100 \mu\text{m}$   $\rightarrow \Phi_{V-NAT} = 50 \text{ mrad}$

**Very large emission angles**  
SISSI: H=70 mrad; V=25 mrad

# Edge Emission

(emitted at the entrance (exit) of a bending magnet due to the rapid variation of the B field)



Edge radiation

**In the Far-Field approximation:**

$$P = \alpha \times I \times \gamma^4 \Theta^2 / (1 + \gamma^2 \Theta^2)^2 \text{ photons s}^{-1}$$

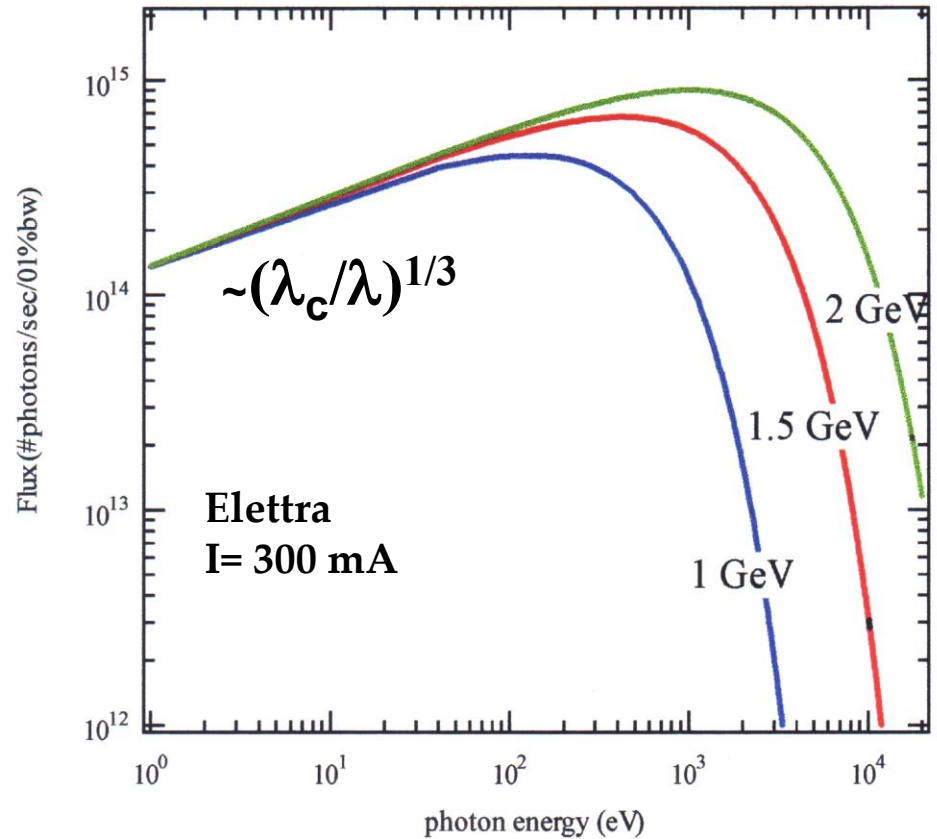
$I$  is the current in amperes,  
 $\Theta$ (rads) the emission angle  
(concentrated in  $\Theta_{\max} \sim 1/\gamma \sim 10$  mrad)

# IRSR FLUX

The IRSR flux and Brilliance depend only on:

- beam current
- source size/emittance
- extraction aperture
- transmission optics

Instead scarcely depend on the machine energy



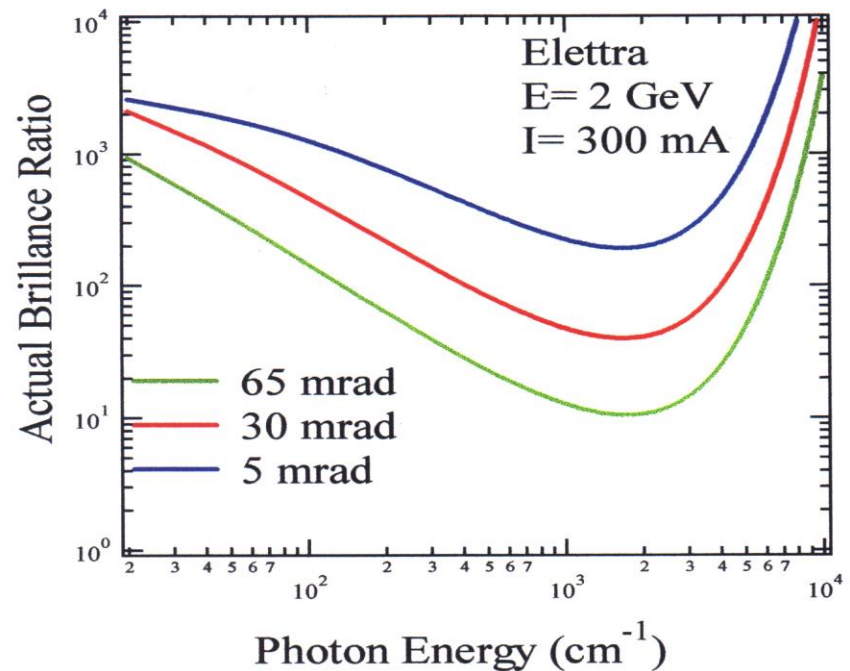
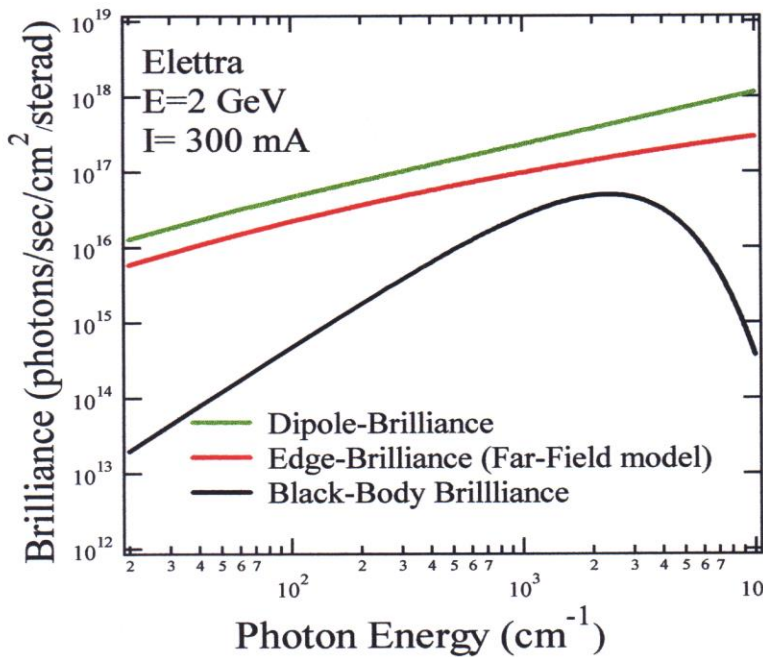


# IRSR Brilliance

The most important figure of merit for IRSR is the **Brilliance**

$$B_{SR} = \frac{d^2 F / d\theta d\varphi}{ASA} \quad (\text{photons}/0.1\%bw/cm^2/\text{str})$$

Where the Actual Source Area is an estimation of the dimension of the source at the exit port (Hulbert and Weber,92; A. Nucara, 1998)



Limiting Noise

$$\%N = \frac{100A^{1/2} D^*}{B(\nu) \Delta\nu \varepsilon t^{1/2} \xi}$$

Where: A detector area, D\* detectivity, **B** brilliance,  $\Delta\nu$  bandwidth,  $\varepsilon$  etendue, t measuring time,  $\xi$  optical efficiency

# Advantages of IRSR

## ADVANTAGES:

**FLUX GAIN**

**BROAD BAND**

**LINEAR & CIRCULAR  
POLARIZATION**

**BRILLIANCE GAIN**

**Diffraction Limited Spatial Resolution**

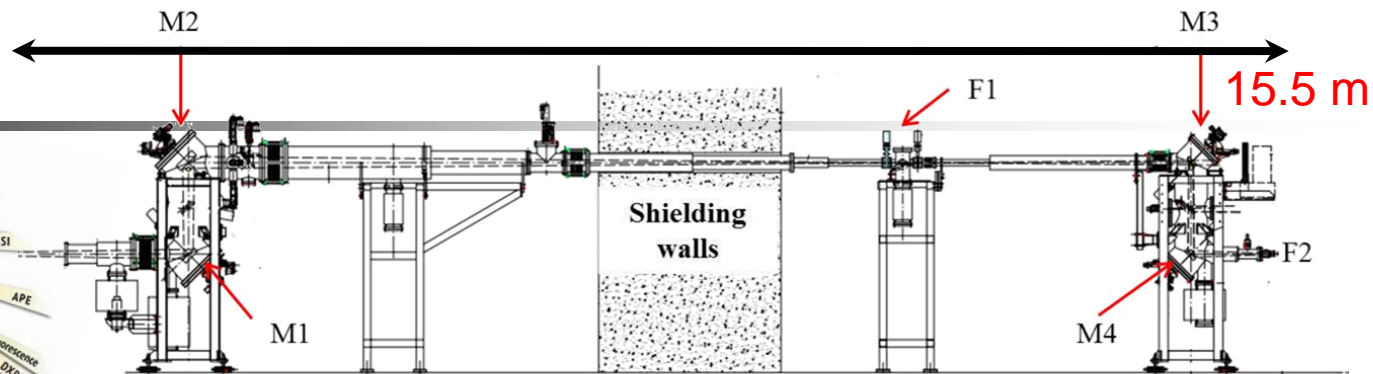
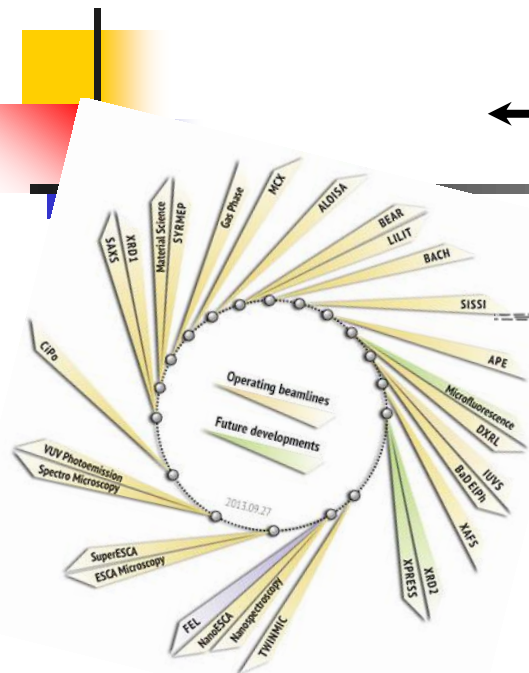
**Better Signal-to-Noise**

**Faster Data Collection**

**SPECTROSCOPY**

**MICROSCOPY**

# SISSI (Source for Imaging and Spectroscopy in the Infrared)

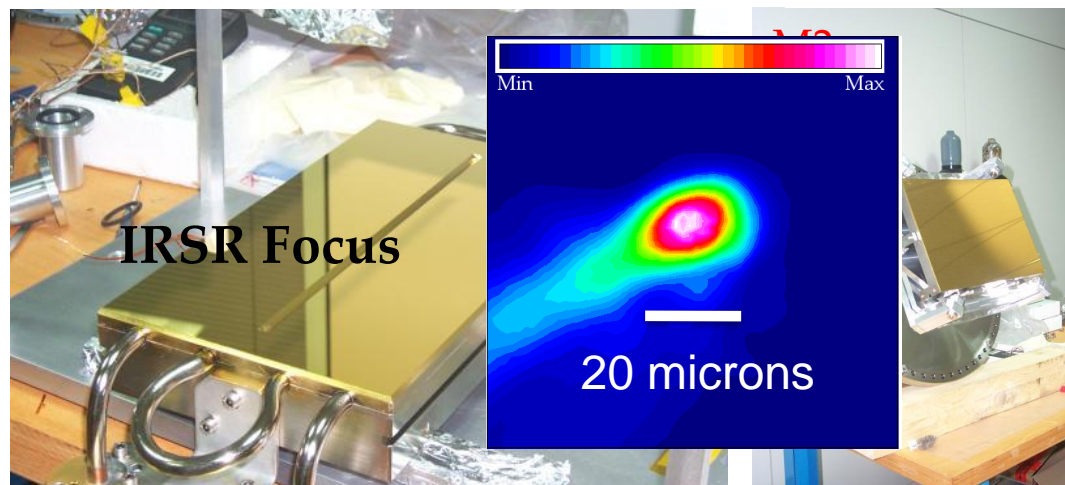


Elettra  
Sincrotrone  
Trieste

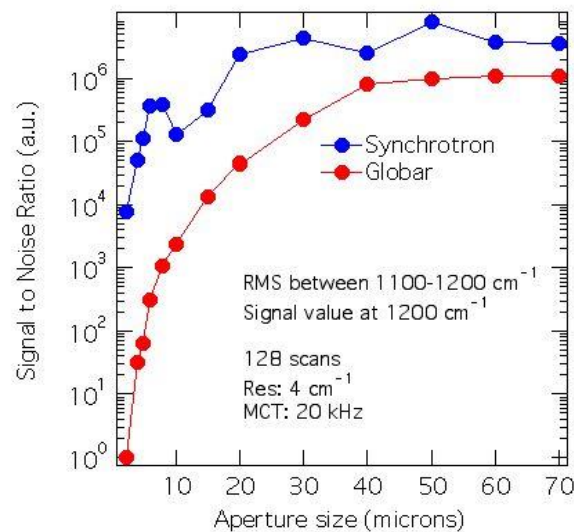
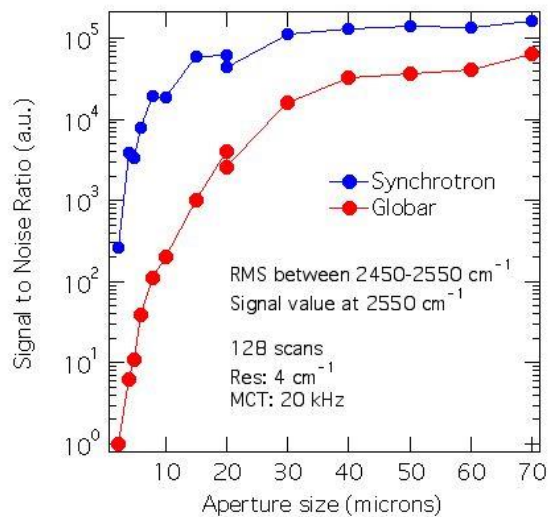
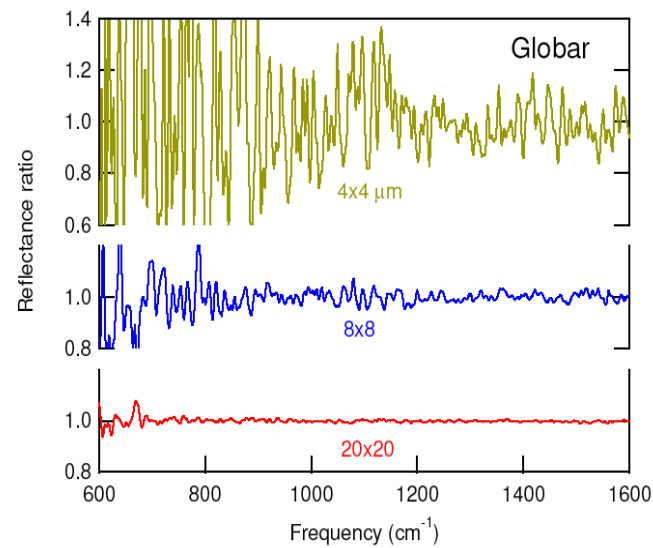
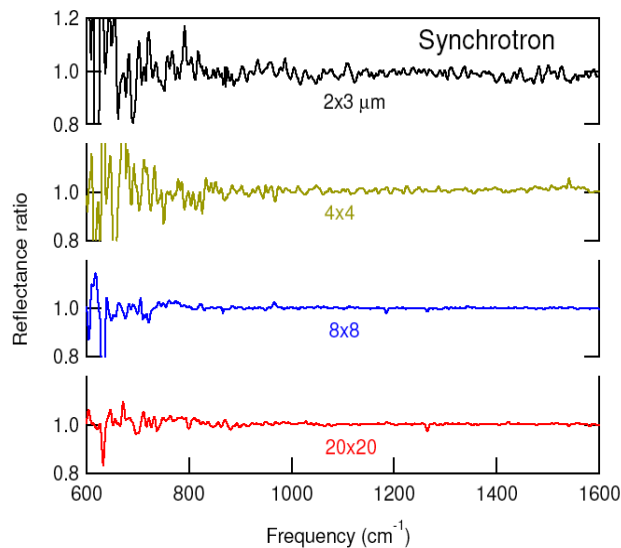


$65 \pm 5$  (H) x  $25$  (V) mrad

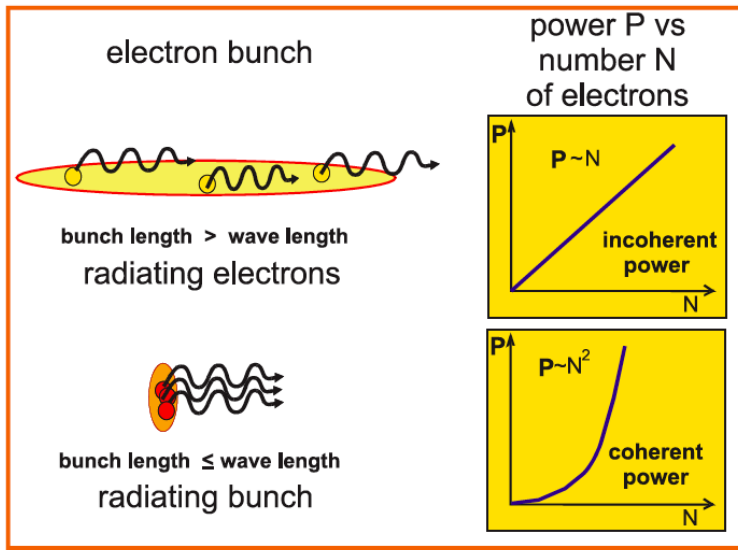
	Figure	Dimension HXV (cm <sup>2</sup> )
M1	Plane	30X15
M2	Ellipsoidal	35X18
M3	Plane	15X8
M4	Ellipsoidal	16X10



# Brilliance gain at SISSI



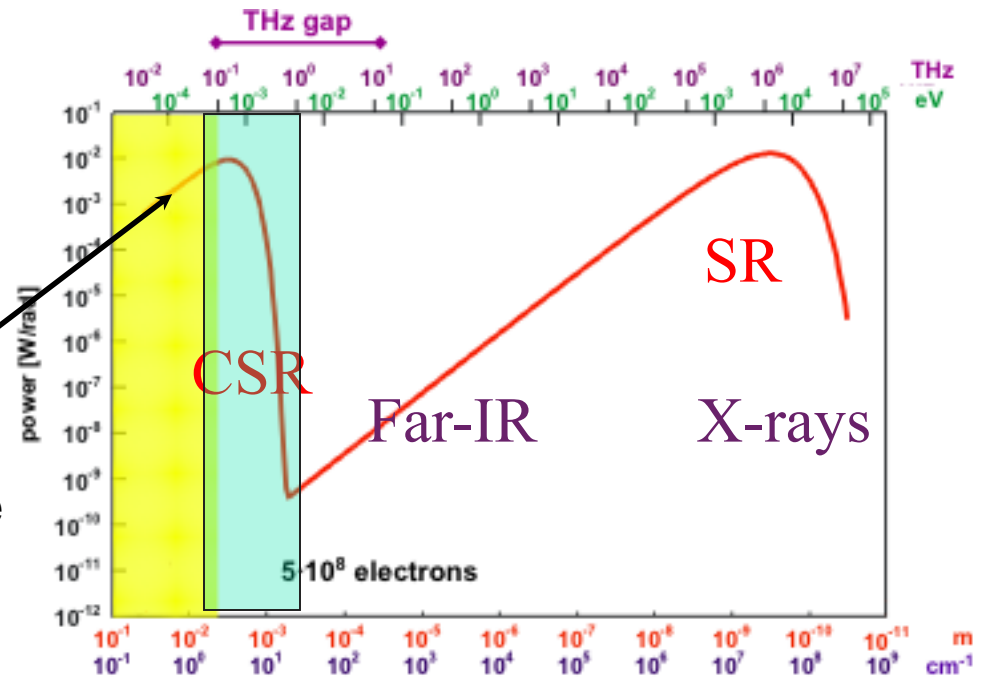
# Increasing the Far-IR Flux: Coherent vs Incoherent Synchrotron Radiation



Flux:

$$I = I_{incoh} + I_{coh} = (N(1 - f_v) + N^2 f_v) I_{incoh}$$

$$f_v = \left| \int n(z) e^{i\pi \cos(\theta) z v} dz \right|^2 \text{ Bunch form factor}$$



Diffraction due to chamber size

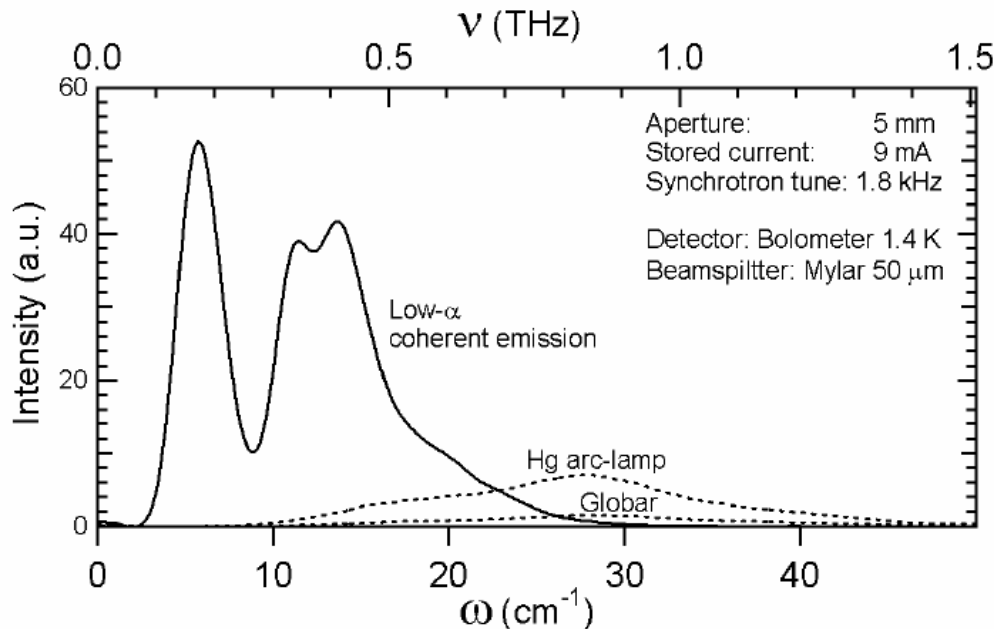
# Production of Coherent Synchrotron Radiation

## Two main methods in a Synchrotron Machine

### Low- $\alpha$ mode

Needed to change the magnetic optics:  
Only dedicated runs

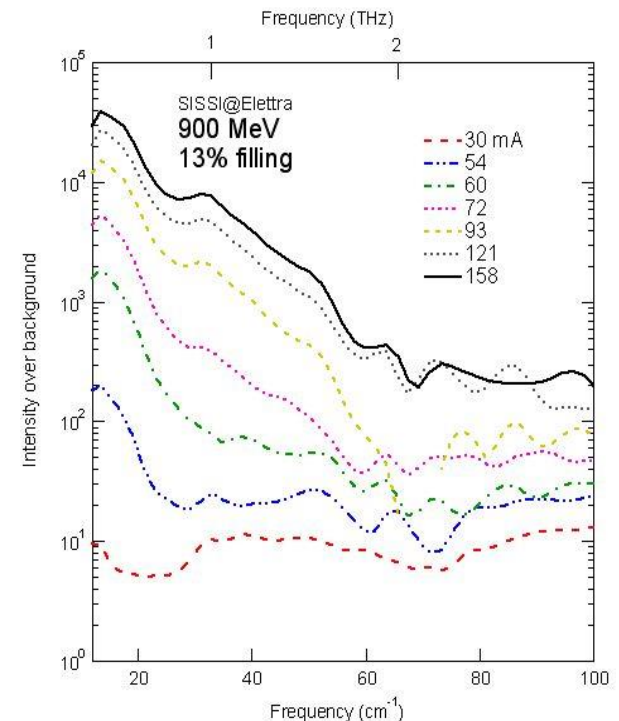
Momentum compaction factor  $\alpha$  :  $\Delta p/p = \alpha = \sigma/L$   
Where  $\sigma$  is the bunch length and  $L$  is the length of the ideal trajectory inside the machine



### Low-e beam energy

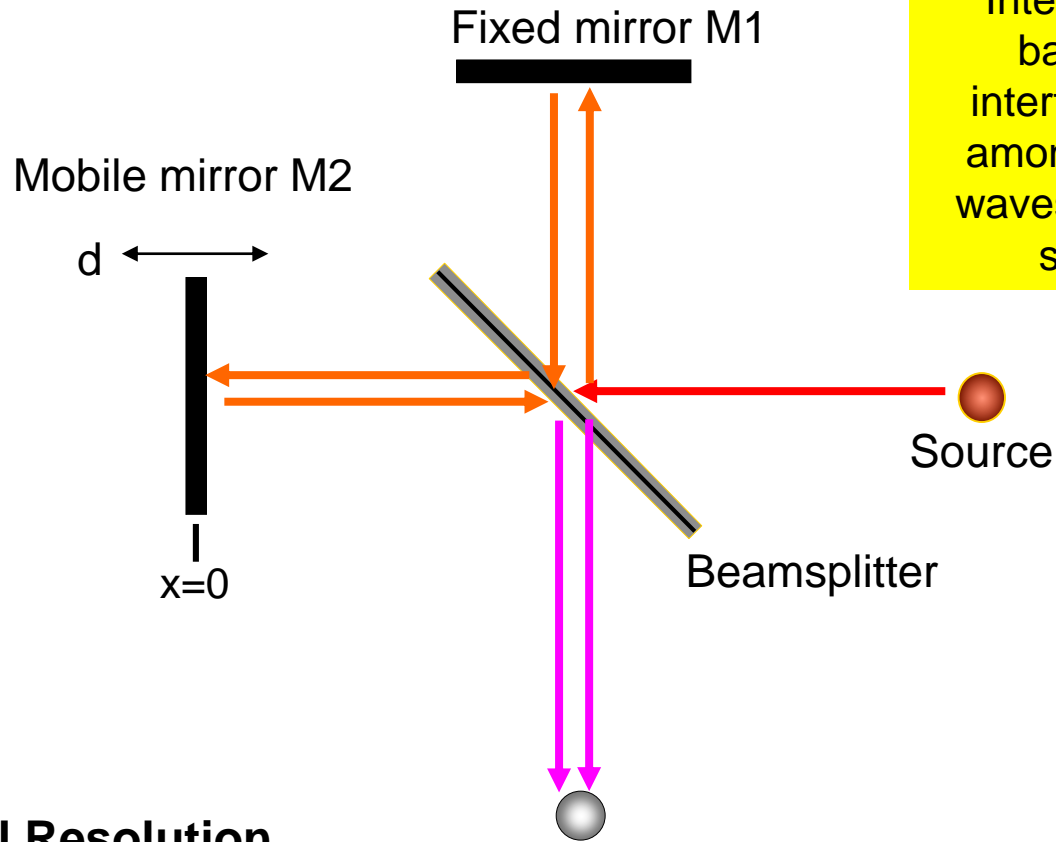
Injected the machine at low-E:  
Reducing life-time and stability

$$\sigma = E^{2/3}$$



# Instrumentation I

## Measuring a source power spectrum: Michelson Interferometer



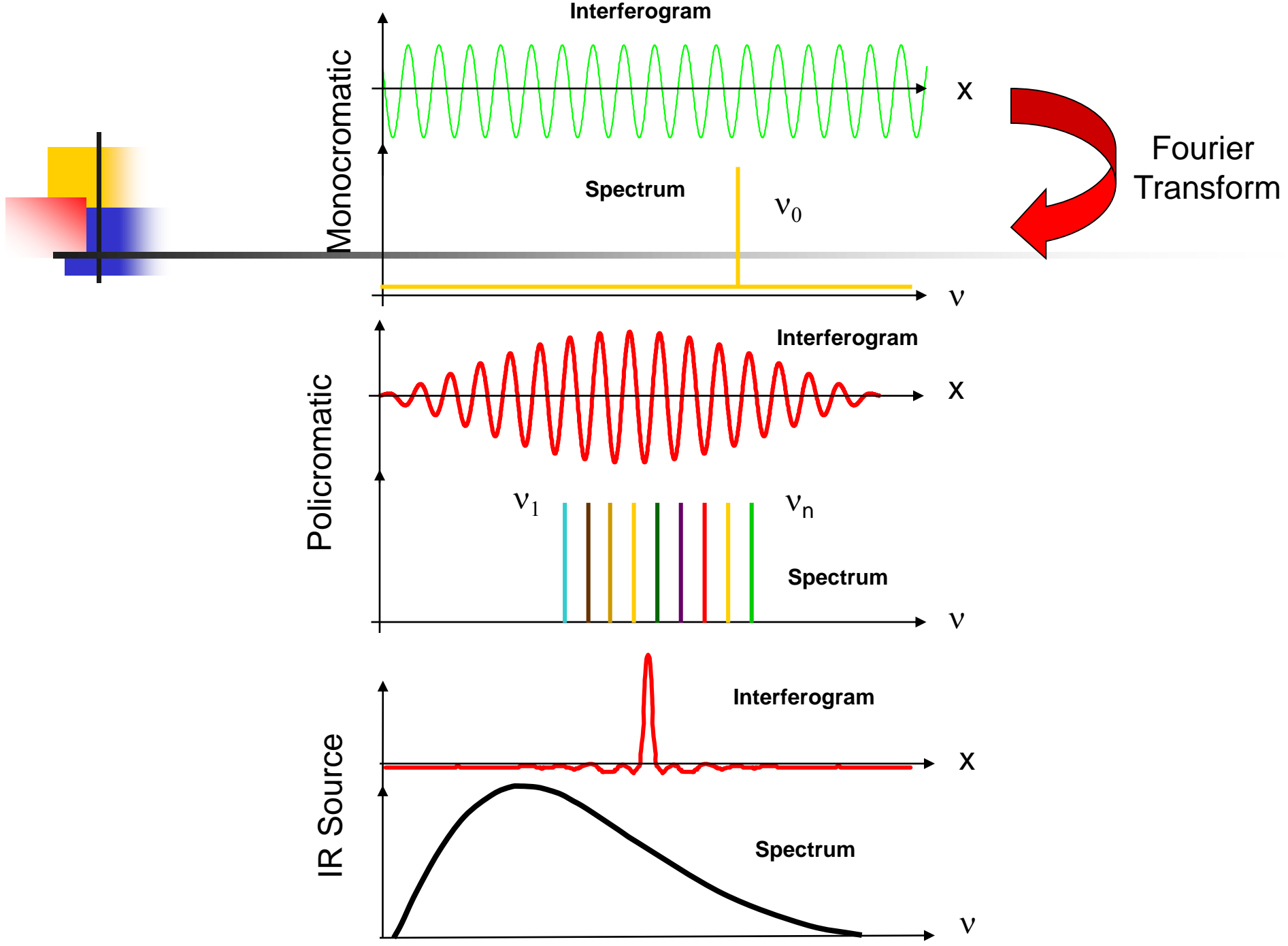
A Michelson Interferometer is based on the interference effect among the two *em* waves at the beam-splitter site

**Spectral Resolution**

$$\Delta\nu \sim 1/d \text{ (cm}^{-1}\text{)} \sim 0.001 \text{ cm}^{-1} \sim 1\mu\text{eV}$$

Detector  $\rightarrow$  Measure of the figure of interference  
**Interferogram**







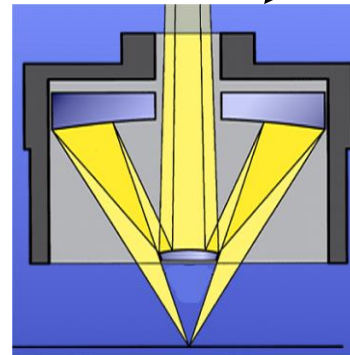
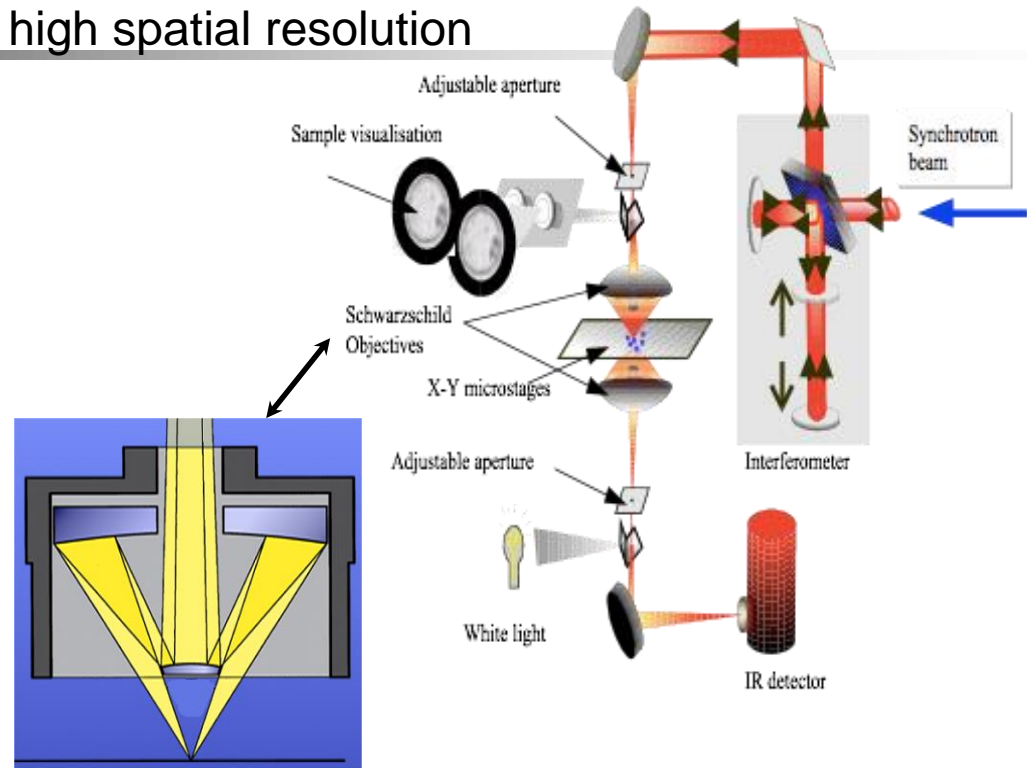
# Instrumentation II

## Infrared Microscopy

**Infrared Microscope---->Beam Condenser**

Visualize and measure small and/or no-homogenous sample (size < 100 μm) with a high spatial resolution

**Bruker-Hyperion**



**In the IR spatial Resolution is determined by diffraction**

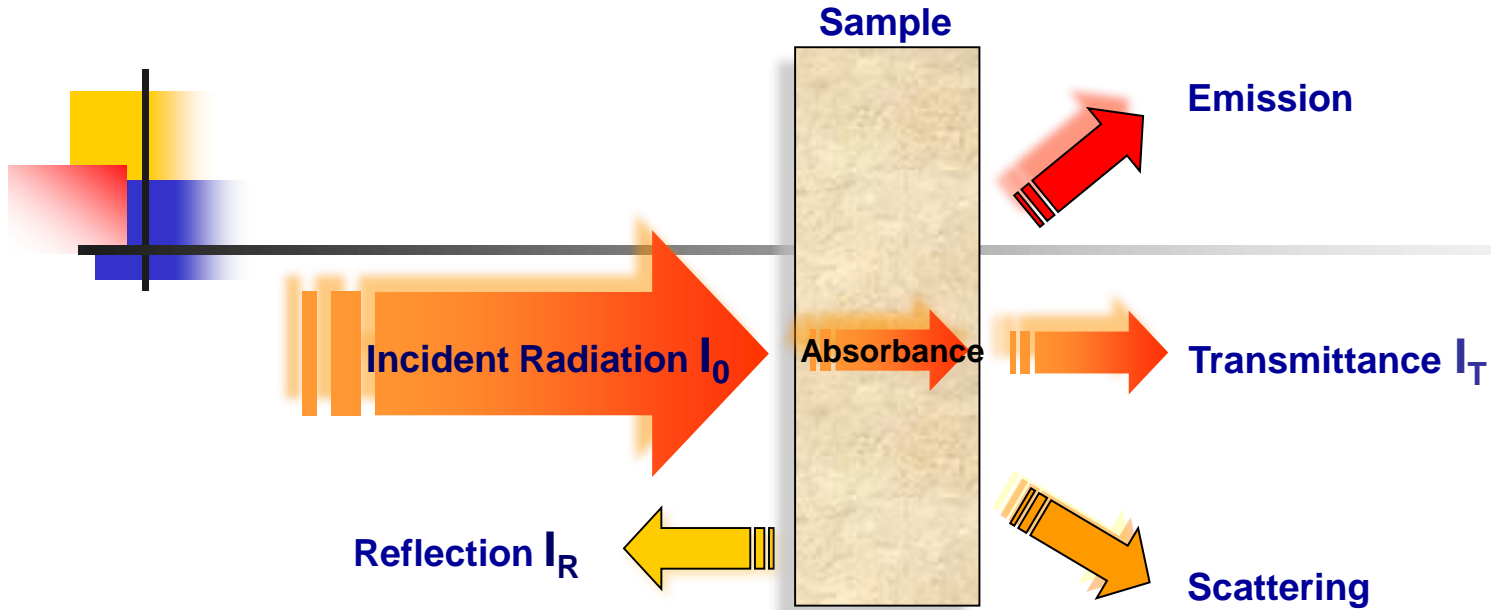
$$\delta = 0.61 \frac{\lambda}{NA} \approx \lambda$$

**For example with a 36x objective with NA=0.5, one obtains:**

at  $\lambda = 10 \mu\text{m}$  ( $1000 \text{ cm}^{-1}$ ):  $12 \mu\text{m}$

at  $\lambda = 2.5 \mu\text{m}$  ( $4000 \text{ cm}^{-1}$ ):  $3 \mu\text{m}$

# Experimental Techniques



**Reflectivity, Transmittance, and Absorption  $R+T+A=1$**

$$R(\omega) = \frac{I_R(\omega)}{I_0(\omega)}$$

$$R(\omega) = \frac{(n-1)^2 + k^2}{(n+1)^2 + k^2}$$

**Via Kramers-Kronig Transformation**  
real and imaginary part of the optical response functions ( $n$ ,  $\varepsilon$ ,  $\sigma$ ) can be obtained

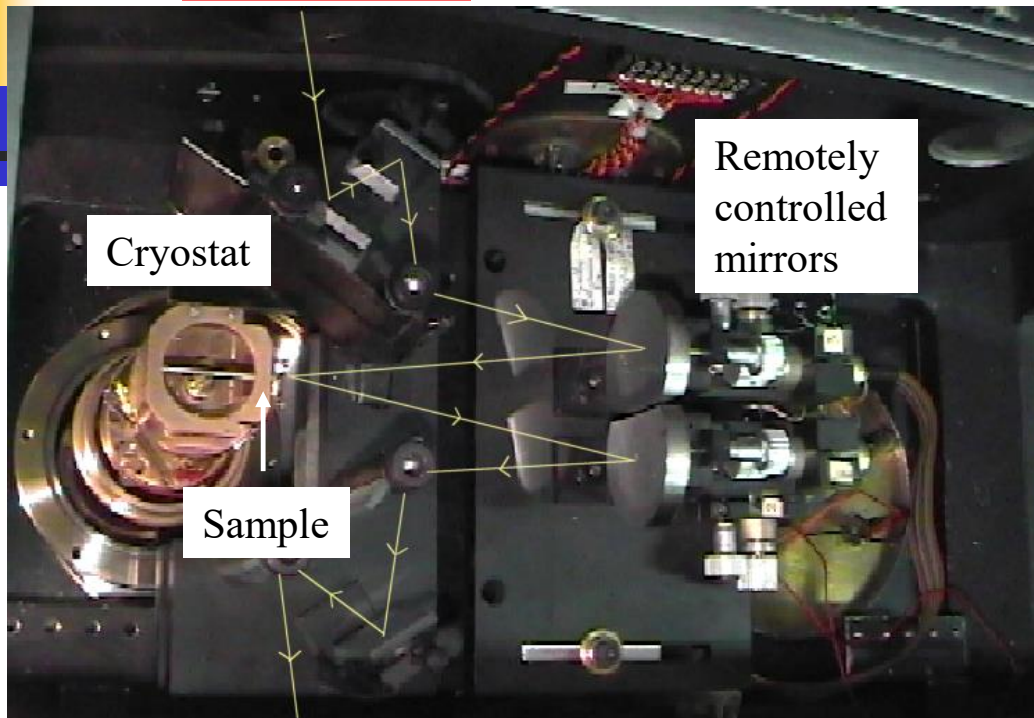
$$\tilde{n} = \sqrt{\tilde{\varepsilon}}$$

$$\varepsilon_1 = n^2 - k^2 = \varepsilon_\infty - \frac{4\pi}{\omega} \sigma_2$$

$$\varepsilon_2 = 2nk = \frac{4\pi}{\omega} \sigma_1$$

# Reflectivity experiments

Interferometer



Reference:  
gold evaporated *in situ*

Reflectivity:

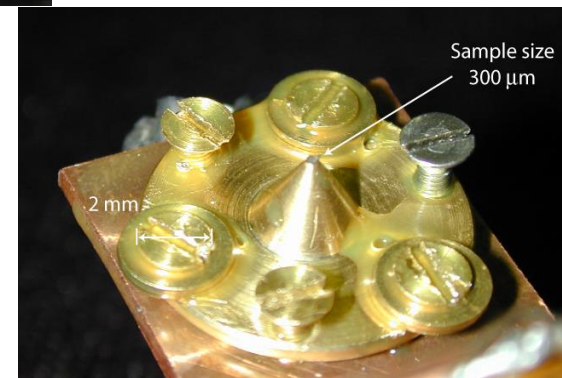
$$R = I_R^{\text{crys}} / I_R^{\text{gold}}$$

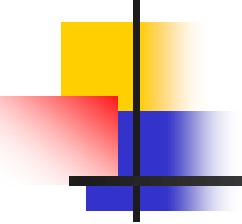
Kramers-Kronig transf.

optical conductivity  
 $\sigma(\omega)$

Detector

Single crystals may be very small:



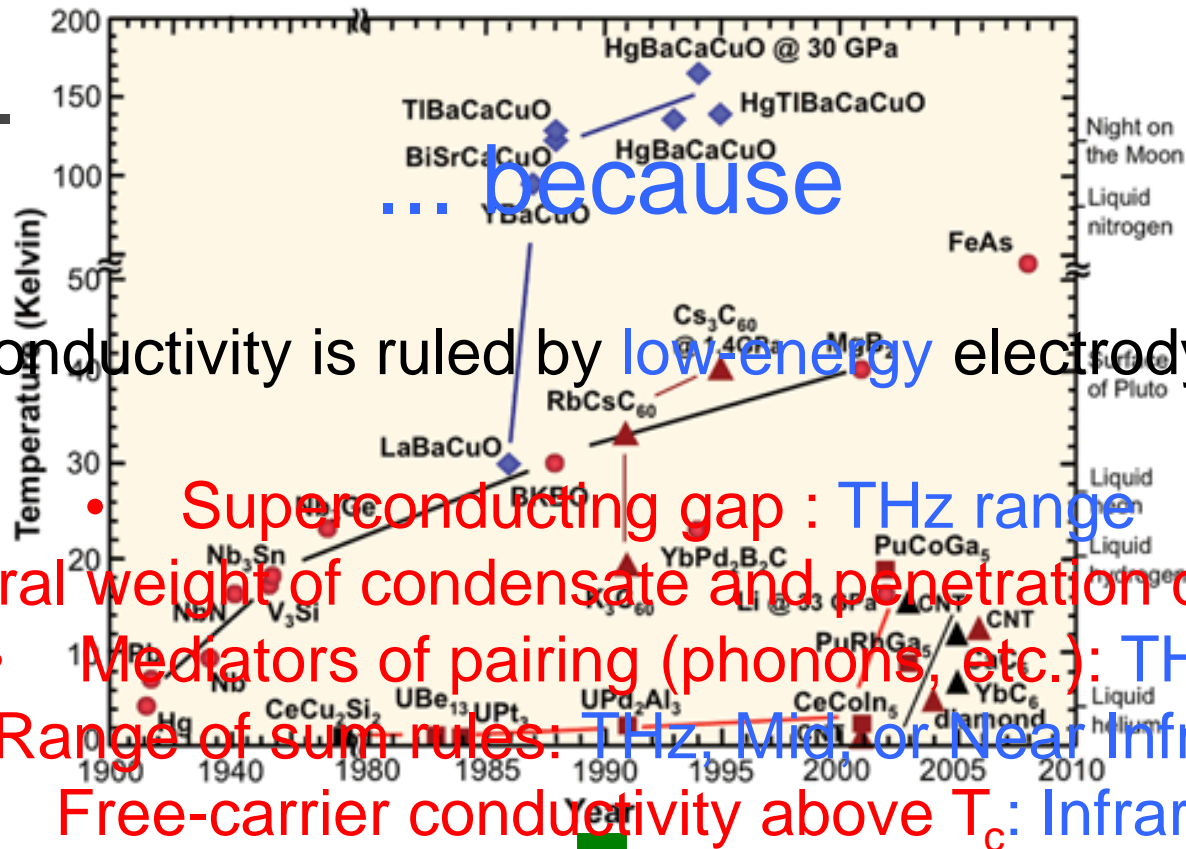


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# Solid-State Applications I Superconductivity

**(FLUX GAIN)**

# Superconductivity today

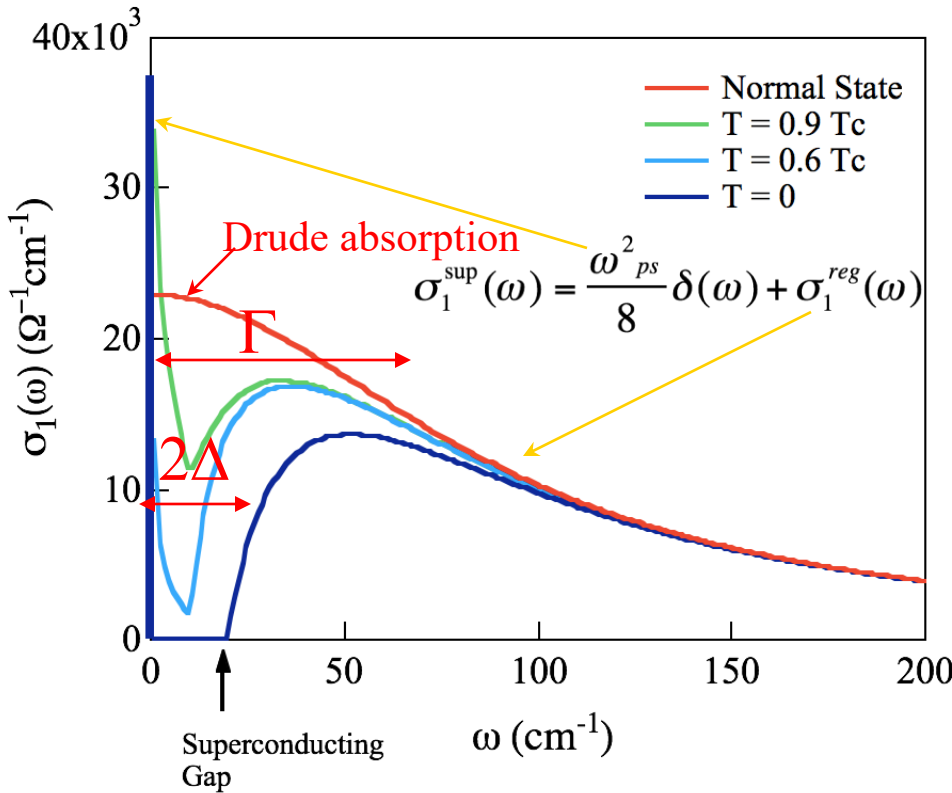
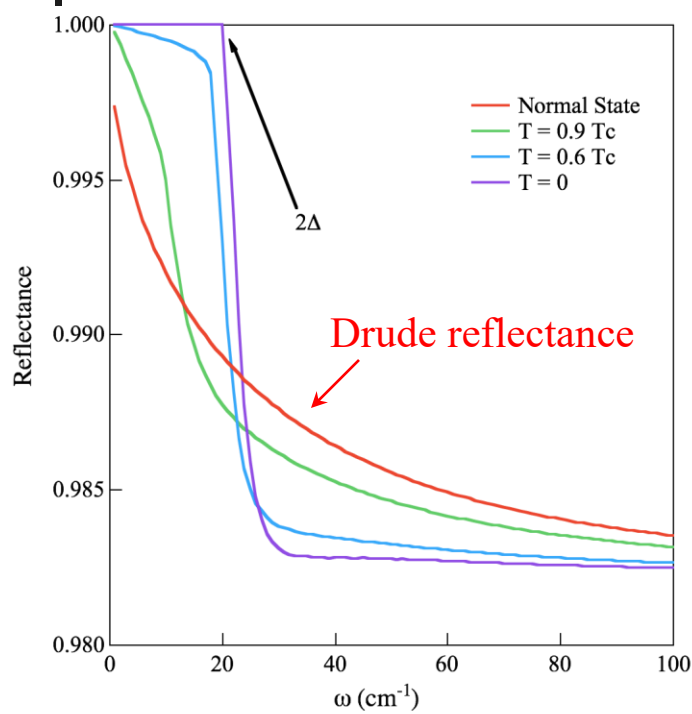


Infrared and THz spectroscopy plays a fundamental role

# Basic optics of Superconductors

Minimum excitation energy:  
Cooper-pair breaking  $2\Delta$

- Superconducting gap observed if:
- sample in the dirty-limit ( $2\Delta < \Gamma$ )
- Cooper pairs in **s-wave** symmetry

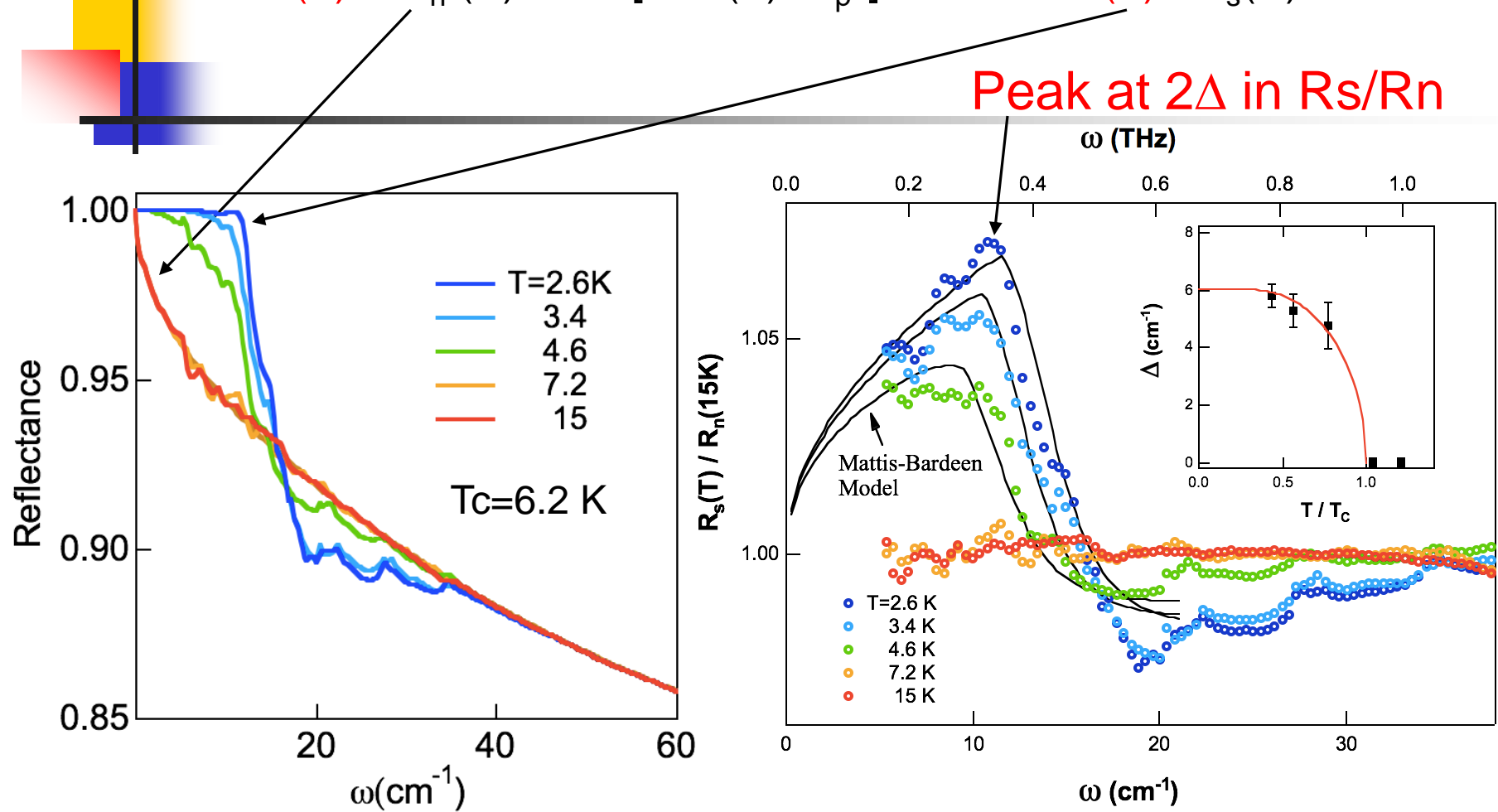


$$\int [\sigma_1(\omega, T > T_c) - \sigma_1(\omega, T < T_c)] d\omega = \omega_{ps}^2 / 8 = n_s e^2 / m^* \rightarrow \lambda = c / \omega_{ps}$$

**Ferrel-Glover-Tinkham Rule**

# THz Reflectivity of Superconducting Diamond

$$\omega \leq \Gamma(T) : R_n(\omega) = 1 - [8\omega\Gamma(T)/\omega_p^2]^{1/2} \quad \omega \leq 2\Delta(T) : R_s(\omega) = 1$$



**s-wave Dirty-Limit Regime;  $2\Delta(2.6 \text{ K}) = 12 \pm 1 \text{ cm}^{-1} \longrightarrow 2\Delta/k_B T_c = 3.2 \pm 0.5$**



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# **Solid-State Applications II**

## **Metal-to-Insulator Transition (MIT)**

**(BRILLIANCE GAIN)**



# Insulator to Metal Transitions

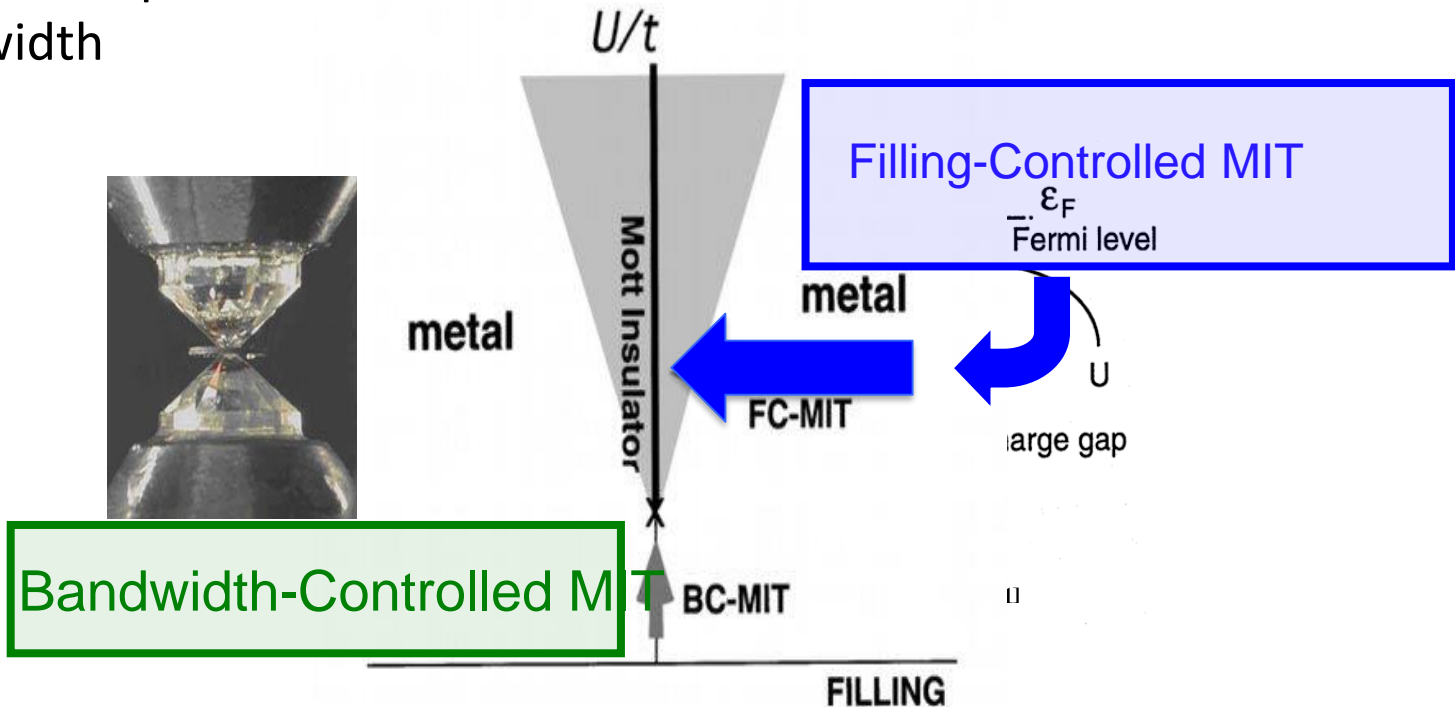
Many materials are insulating although band theory suggests a metallic ground state:  $V_2O_3$ ,  $VO_2$ ,  $NiO$ ,  $NiSe_2$ ,  $La_2CuO_4$ ,  $Cs_3C_{60}$   
 → Strong Electronic Correlations → Hubbard Model

$$H = -t \sum_{\langle ij \rangle \sigma} (c_{i\sigma}^+ c_{j\sigma} + h.c.) + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

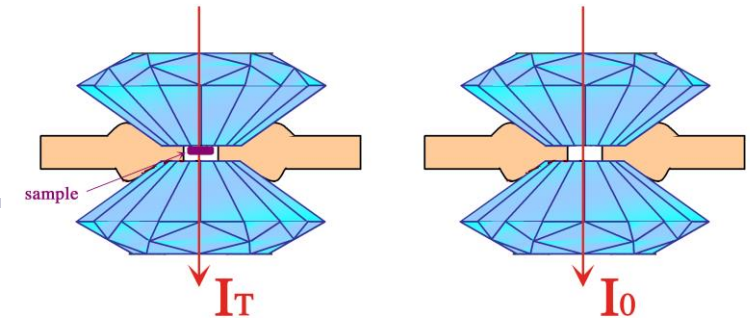
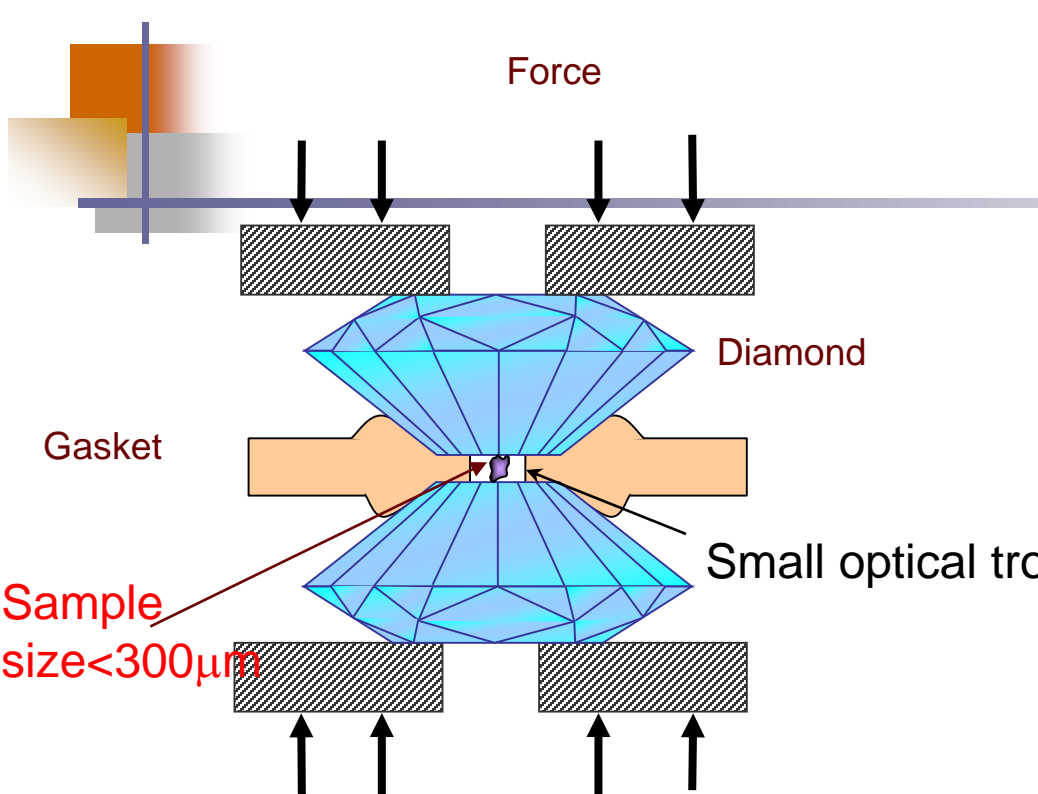
$U$  Coulomb repulsion  
 $t$  Bandwidth

$U$  prevents double on-site occupancy → a gap in the spectra of excitations is induced

How to transform an Insulator in a Metal

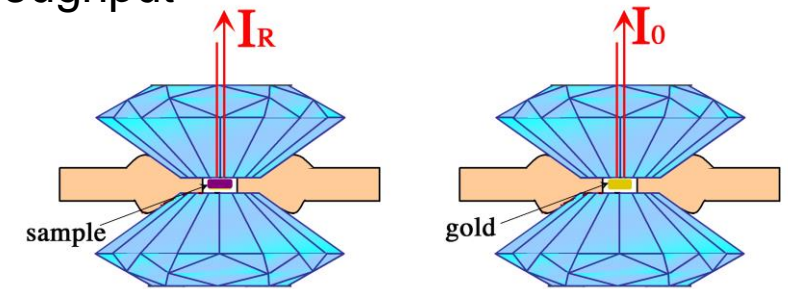


# IRSR Microscopy at high pressures

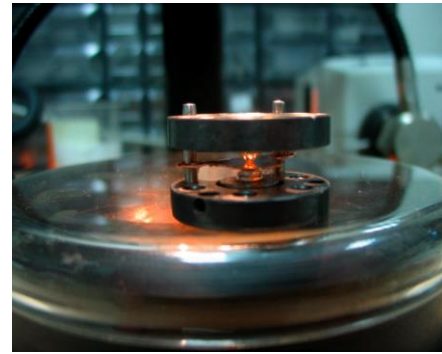
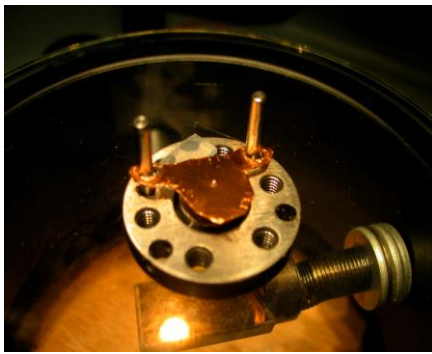


$$T = I_T / I_0$$

$$\text{Op.D.} = -\ln(T) = \alpha d$$

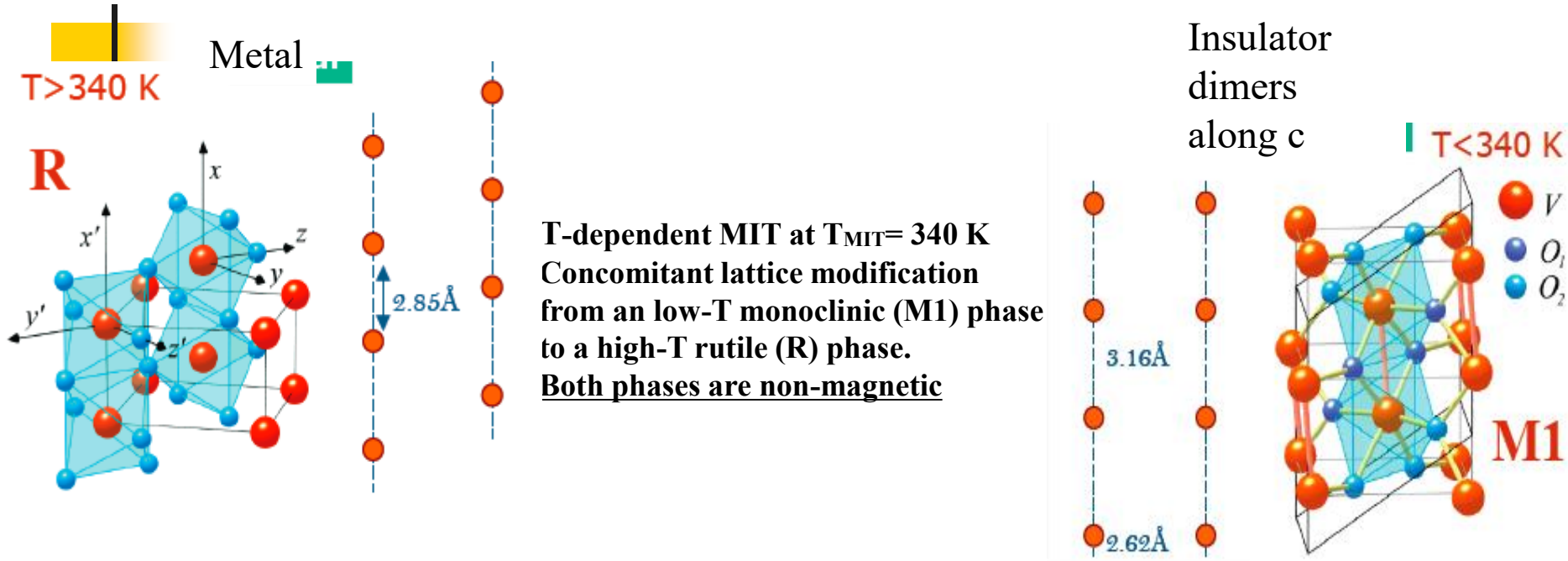


$$R_{\text{diam/sam}} = I_R / I_0$$





# Generalities on Vanadium dioxides $\text{VO}_2$



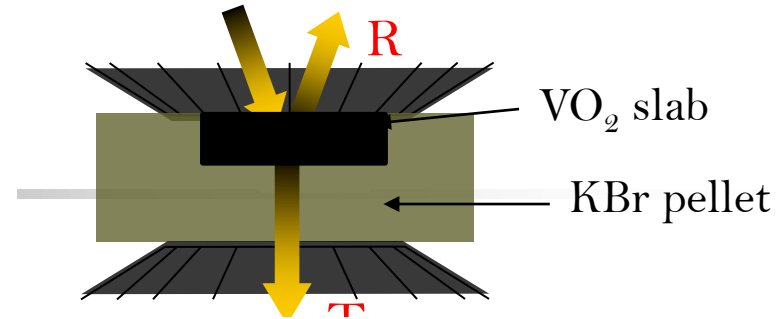
Strong Interplay between electron-lattice and electron-electron interactions

**Driving MIT mechanism Hubbard or Peierls?**

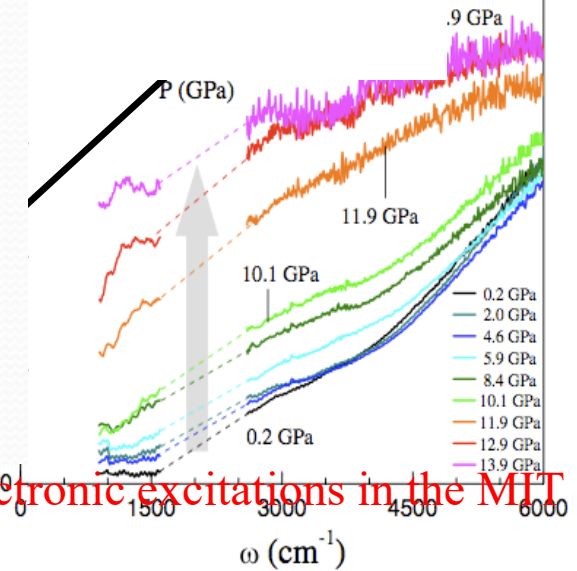
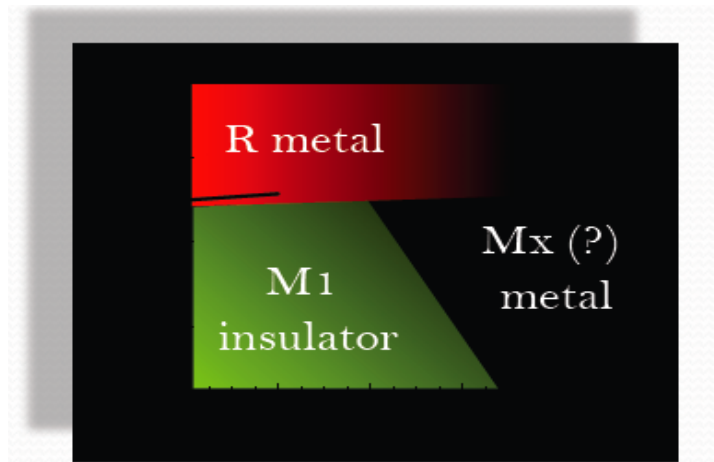
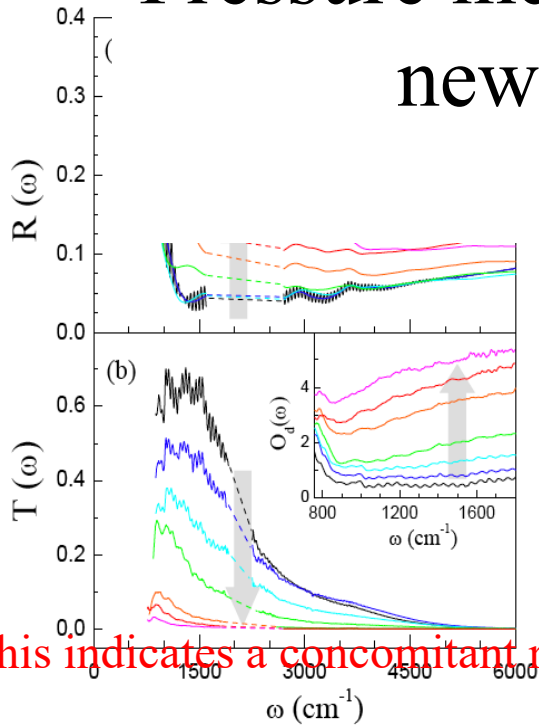
High Pressure may disentangle the two mechanisms

# P-dependent infrared measurements on VO<sub>2</sub>

Simultaneous measurements of reflectance and transmittance at 300 K in the M1 monoclinic insulating phase on a thin VO<sub>2</sub> sample

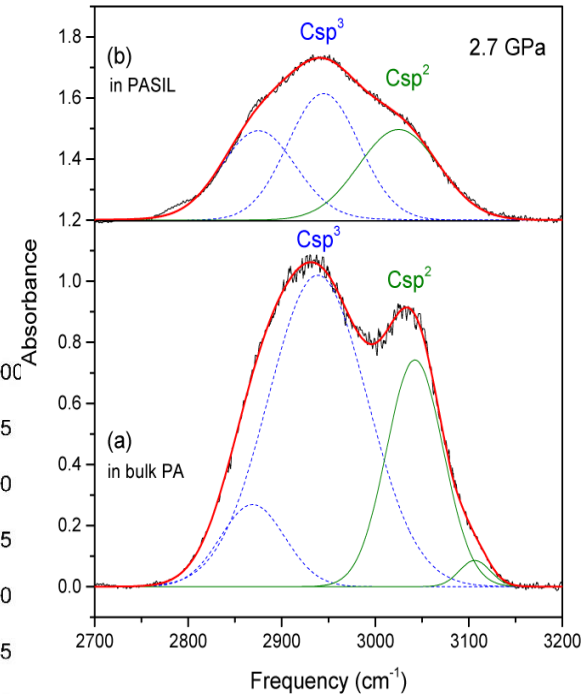
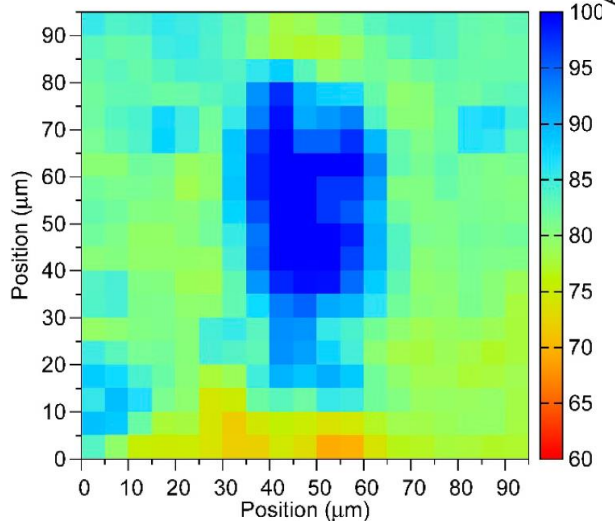
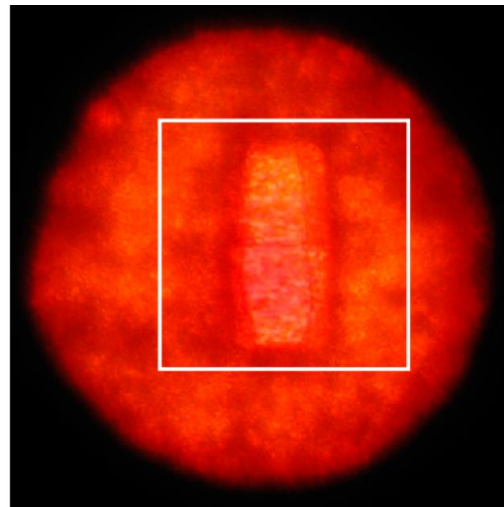
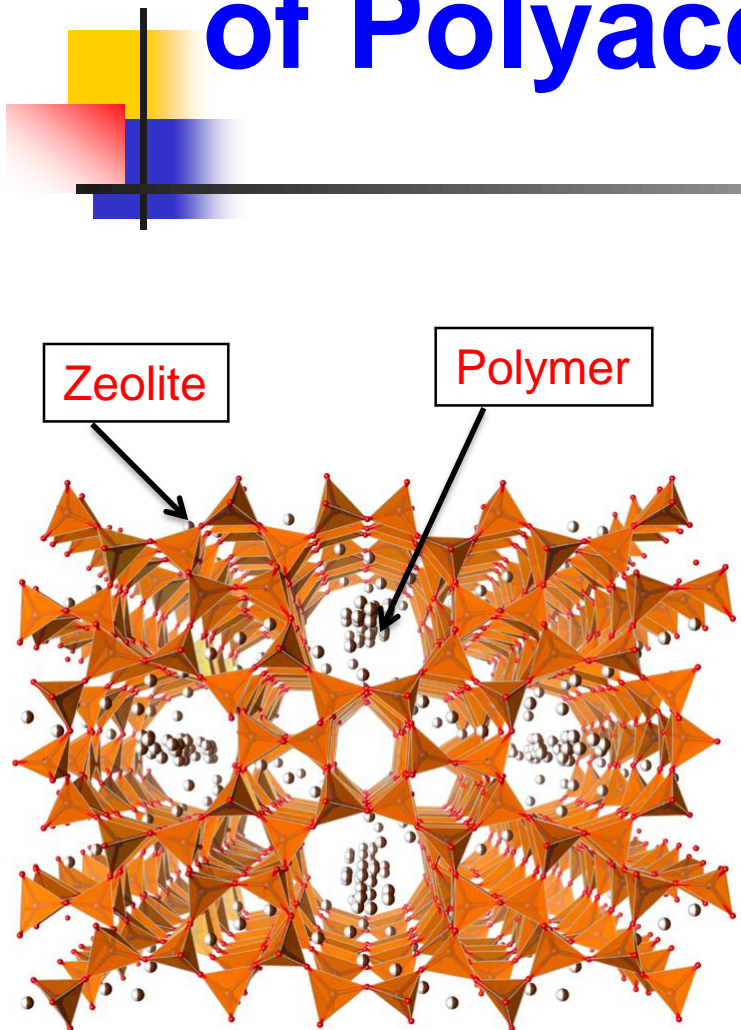


Pressure induces a metallization process in a new monoclinic structure Mx



This indicates a concomitant role of  $\sim 10$  (GPa) phonons and electronic excitations in the MIT

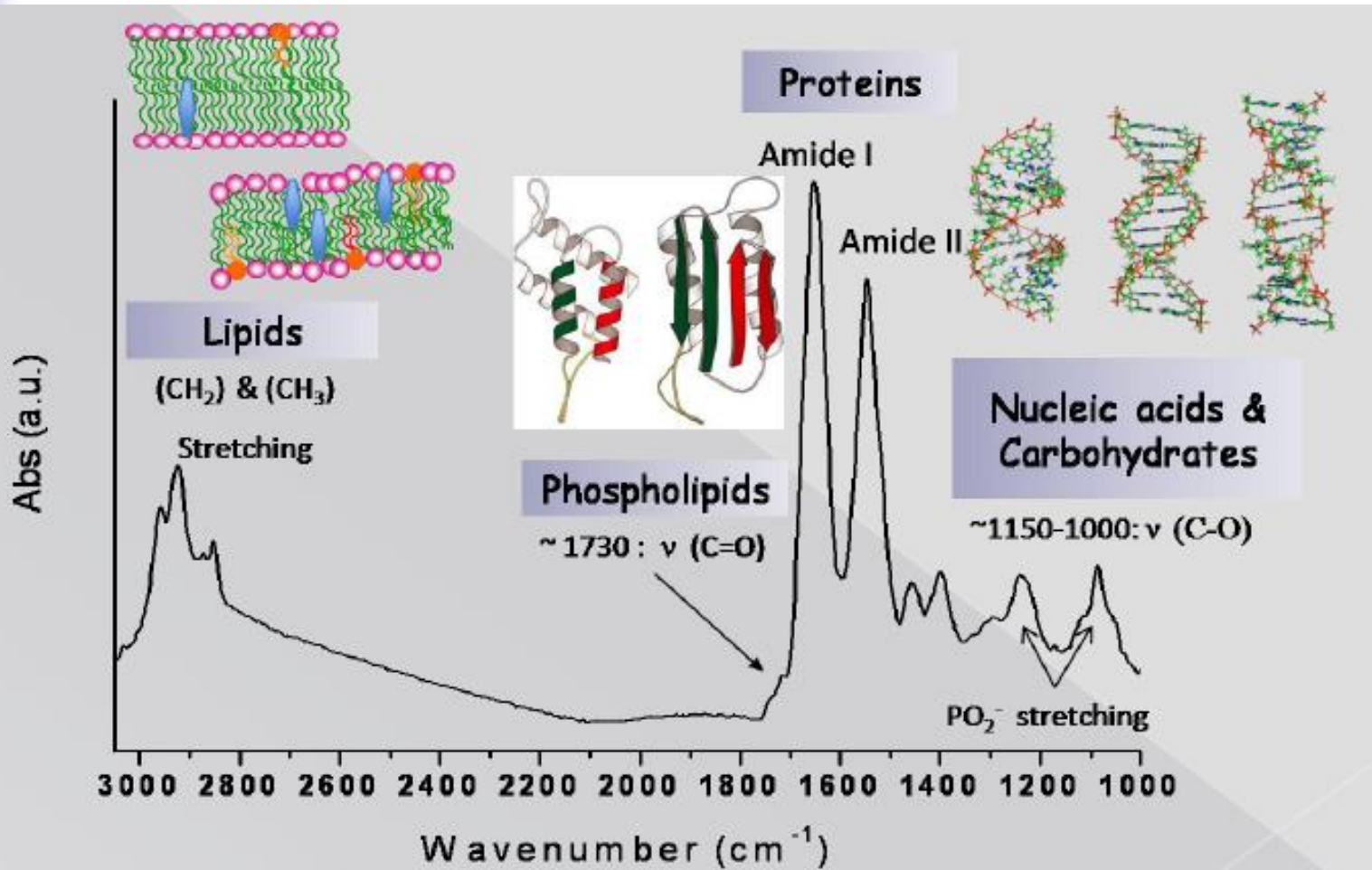
# Pressure Induced Polymerization of Polyacetylene in Zeolite





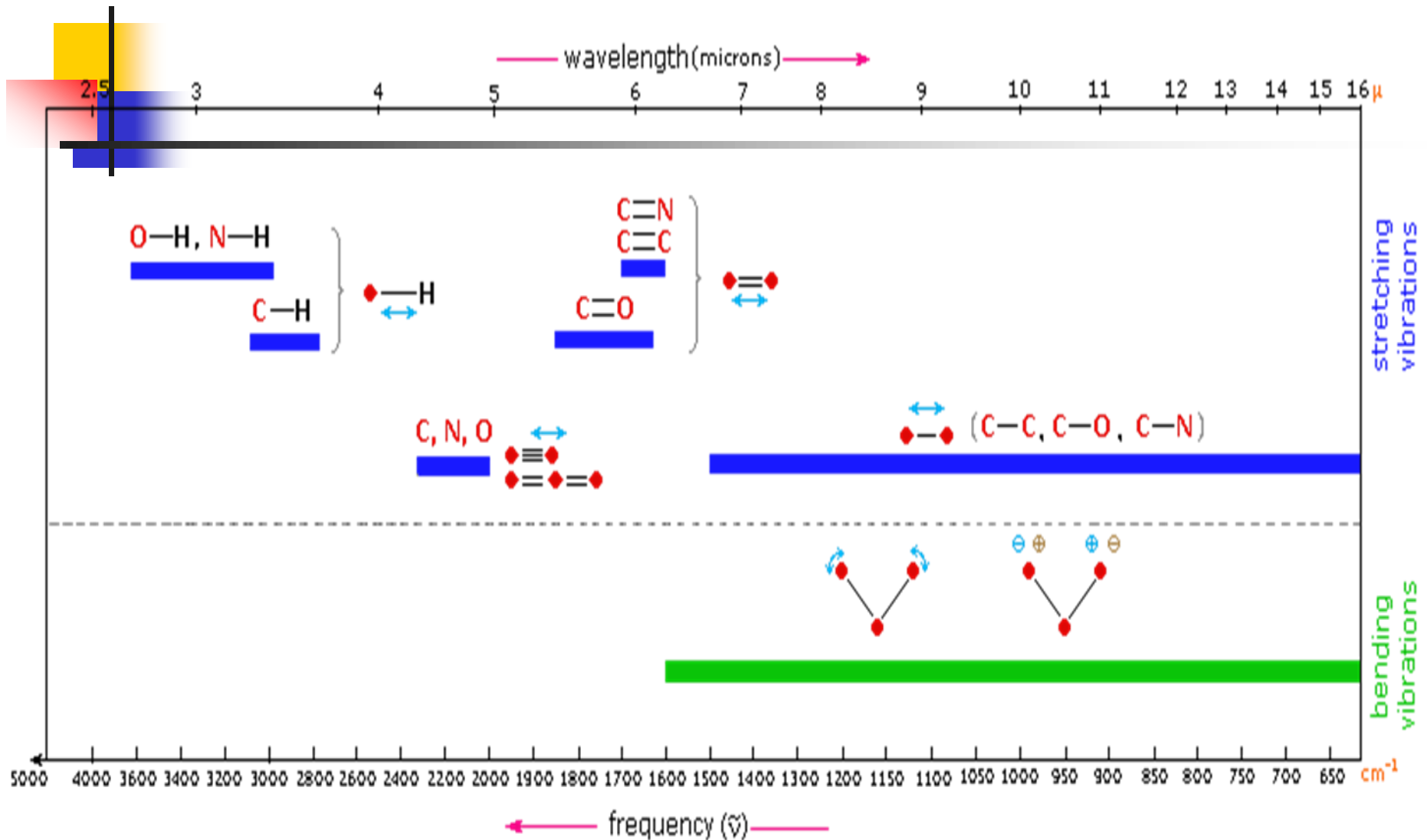
# Medical and Biological Application of IR Microscopy

## How look the IR spectrum of a cell?



Vibration Frequencies correspond to finger-print for the molecule

# Infrared Group frequency region





# IRSR spectrum of a single cell during mitosis

The cell physiology is not altered under IRSR illumination

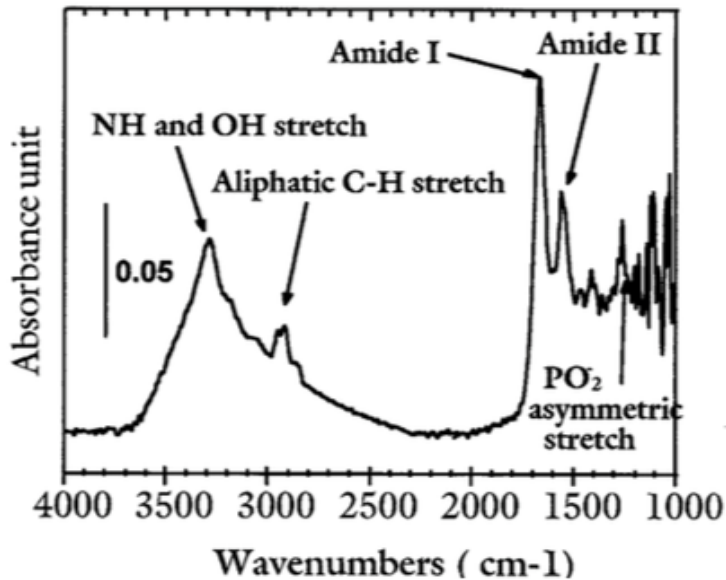
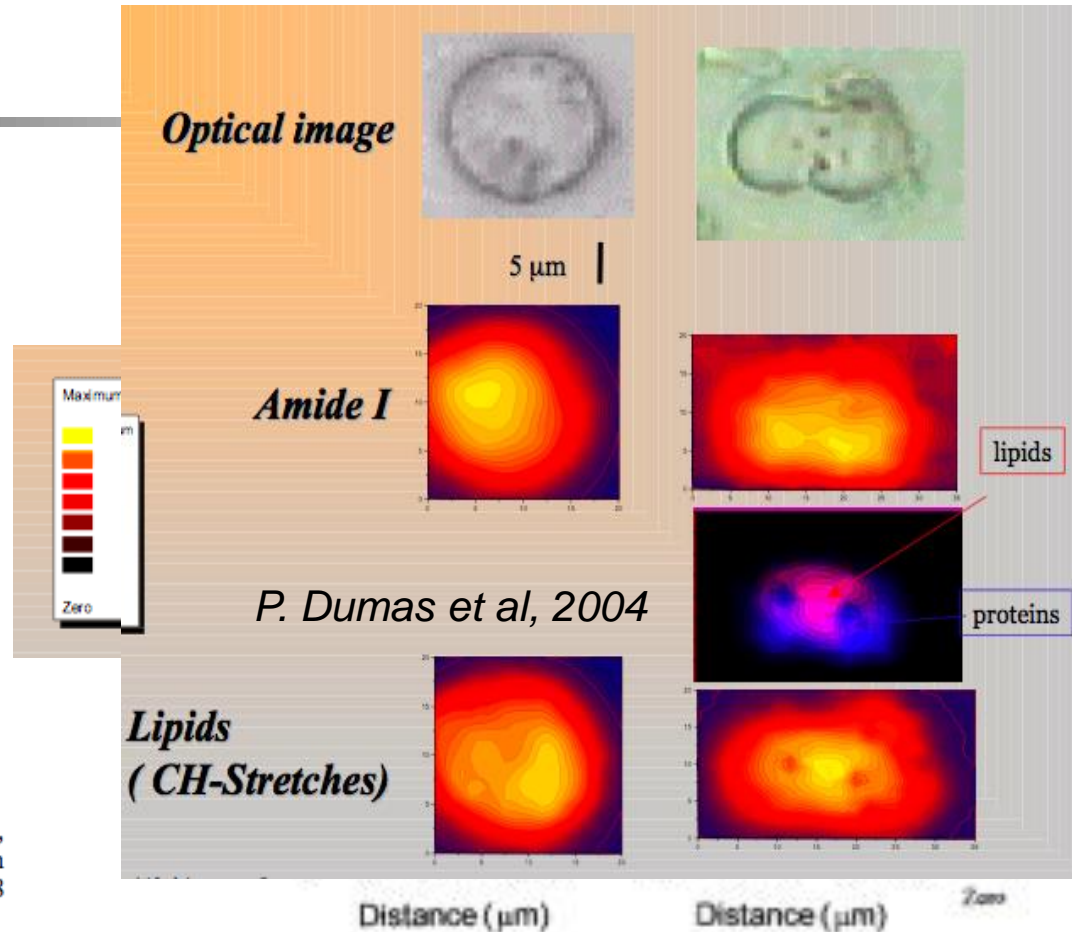
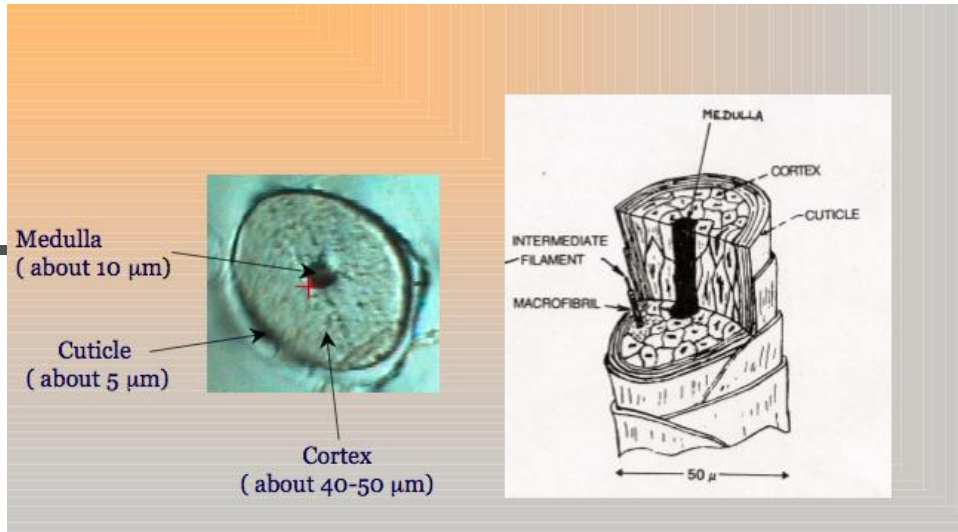


FIG. 1. Infrared spectrum of a mouse UN2 hybridoma B living cell, recorded with an aperture of  $3 \times 3 \mu\text{m}^2$ . The instrumental resolution was set at  $4 \text{ cm}^{-1}$ , and the spectrum displayed is the result of 128 co-added scans (the total recording time is 55 sec).



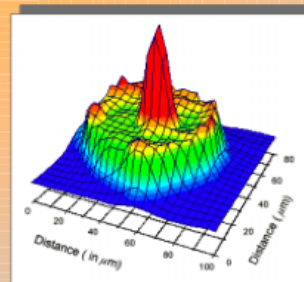
Spatial distribution of proteins and lipids during the cell mitosis

# Studying hair by IRSR microscopy

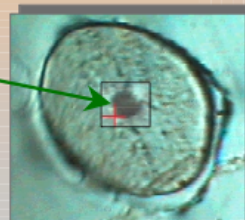
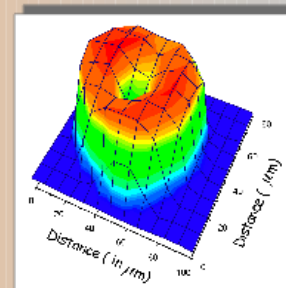


*Intern.J. of Cosmetics Science.* **23** 1-6 (2001) 369-374

Lipid profile



Protein profile

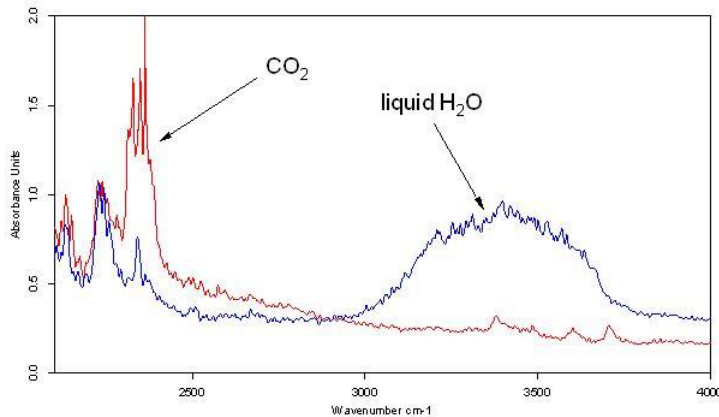


# Geological Applications: liquid inclusion in minerals

## Brilliance gain

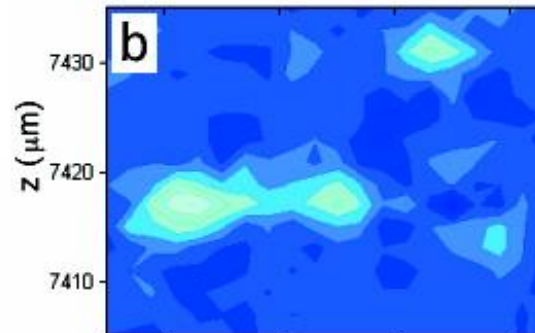
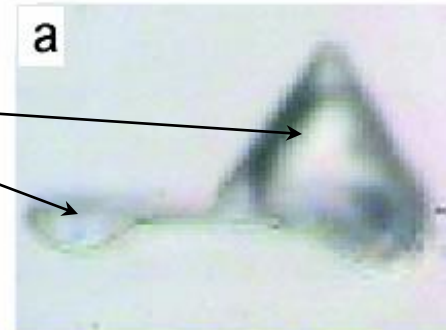
Liquid Inclusion in quartzite  
Mapping with  $3\mu\text{m} \times 3\mu\text{m}$   
(diffraction limited)

### Infrared Spectra

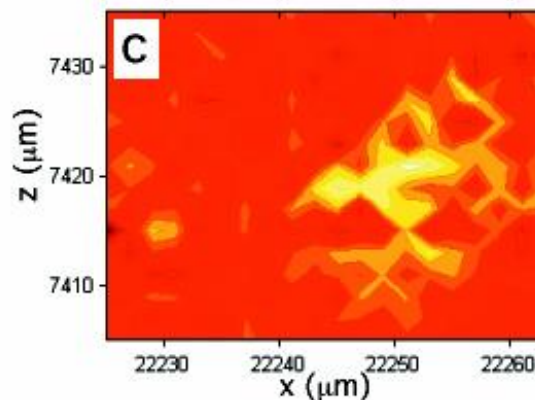


C:\F:\Tr\ccc\rel\25110\Radix\l\Inclusione5_a_3_3_142n A.O	2005/11/25
C:\F:\Tr\ccc\rel\25110\Radix\l\Inclusione5_b_3_3_142n A.O	2005/11/25

Page 1 of 1



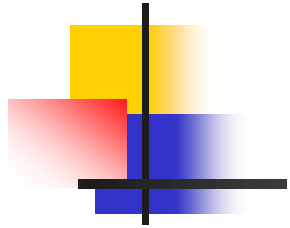
Water Distribution



$\text{CO}_2$  Distribution

# Interstellar micron size dust analysis

*comparison SRS-Black body:*  
3 micron Particles from asteroid "Orgueil"

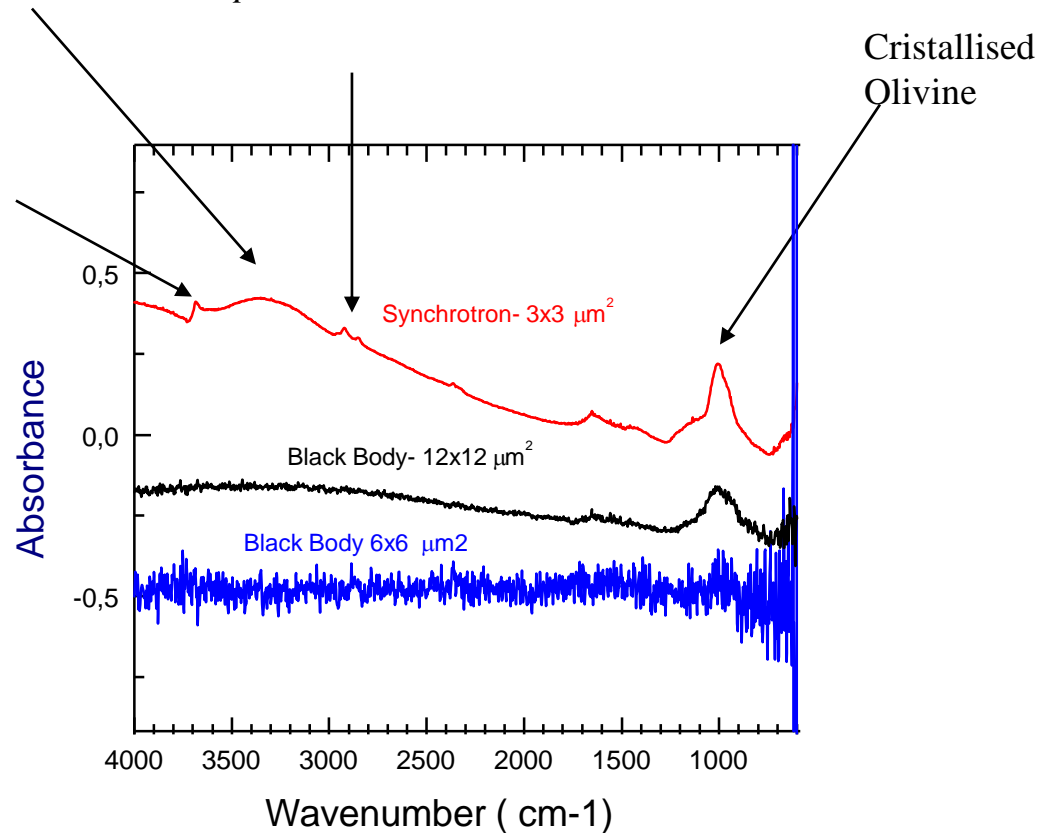


*Molecular water*

*Aliphatic CH*

Cristallised  
Olivine

*OH- silicates*



*Particles collected from the MIR shuttle*

# Recent Developments



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1. THz IV generation sources: Non linear and time-resolved spectroscopy;
2. Beating the diffraction limit → IRSR Nanoscopy

# Linear vs. Non Linear Spectroscopy



## Linear Spectroscopy

---

### **Low Power Source**

**Small Perturbation → Sample retains its equilibrium properties**

## Non linear and Time-Resolved Spectroscopy

### **High Power/Pulse**

**Strong Perturbation → out of equilibrium states → manipulation of matter through em fields**

# Linear versus Non-Linear Optical Response

Actually the linear/non-linear electrodynamics regimes can be estimated through the ratio

$$Q = \left[ \frac{eE}{\omega} \right] / p_F$$

Electromagnetic Momentum

Fermi Momentum

Linear regime  $E_{\text{THz}} \approx 10\text{-}100 \text{ V/cm} \rightarrow Q \ll 1 \longleftrightarrow T = T(\omega) \longleftrightarrow \sigma = \sigma(\omega)$

Non linear regime  $\rightarrow Q = 1$

Putting  $\omega/2\pi = 1 \text{ THz}$  and  $p_F$ ,  $Q = 1$  for  $E_{\text{THz}} \approx 50 \text{ kV/cm} \rightarrow$  then the optical functions start to be dependent on the applied electric field.

For instance:  $T = T(\omega, E_0) \longleftrightarrow \sigma = \sigma(\omega, E_0)$

# THz Sources for Non Linear and Pump-Probe Spectroscopy

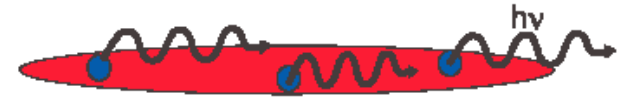
## Figures of merit of a pump source:

- 1) Energy per pulse  $\approx 1 \mu\text{J}$ -10 mJ;
- 2) Pulse duration  $\rightarrow$  sub-ps scale (more relaxed than in VIS-Near-IR)  $\rightarrow$  an excitation starts to exist after half a cycle ( $T \approx 100 \text{ fs}$ -10 ps);
- 3) Rep rate tens of Hz to MHz;
- 4) Frequency tunability;
- 5) Associate electric field 100 KV/cm ( $1 \text{ mV}/\text{\AA}$ ) to 100 MV/cm ( $1 \text{ V}/\text{\AA}$ )  $\rightarrow$  Atomic field;
- 6) Associate magnetic field  $\approx 1 \text{ T}$



# Coherent Radiation from sub-ps electron bunches

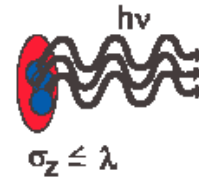
$$\frac{d^2 I}{d\omega d\Omega} = \frac{d^2 I_{sp}}{d\omega d\Omega} [N + N(N-1)F(\omega)]$$



$$\sigma_z > \lambda$$

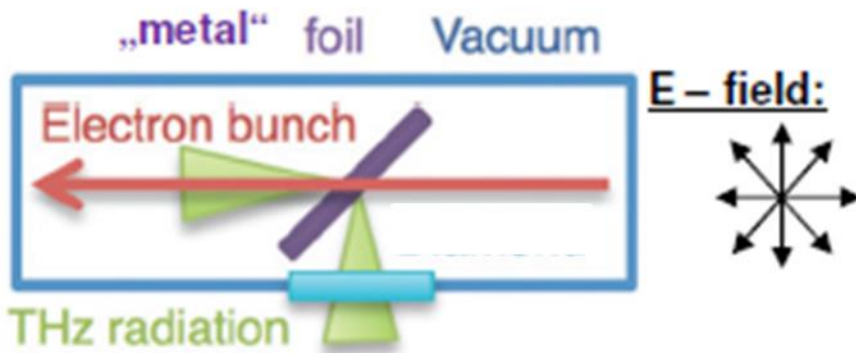
Long bunch emits incoherently

Short bunch emits coherently

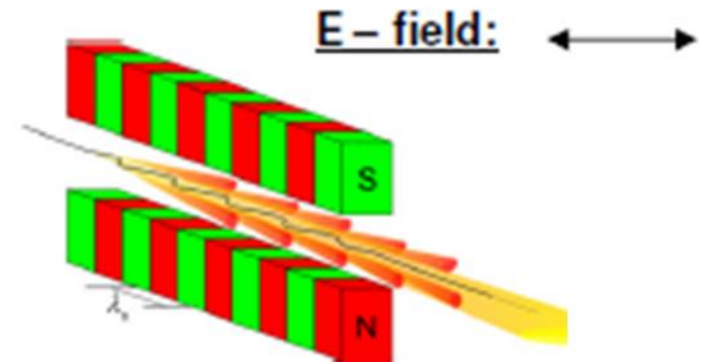


$$\sigma_z \leq \lambda$$

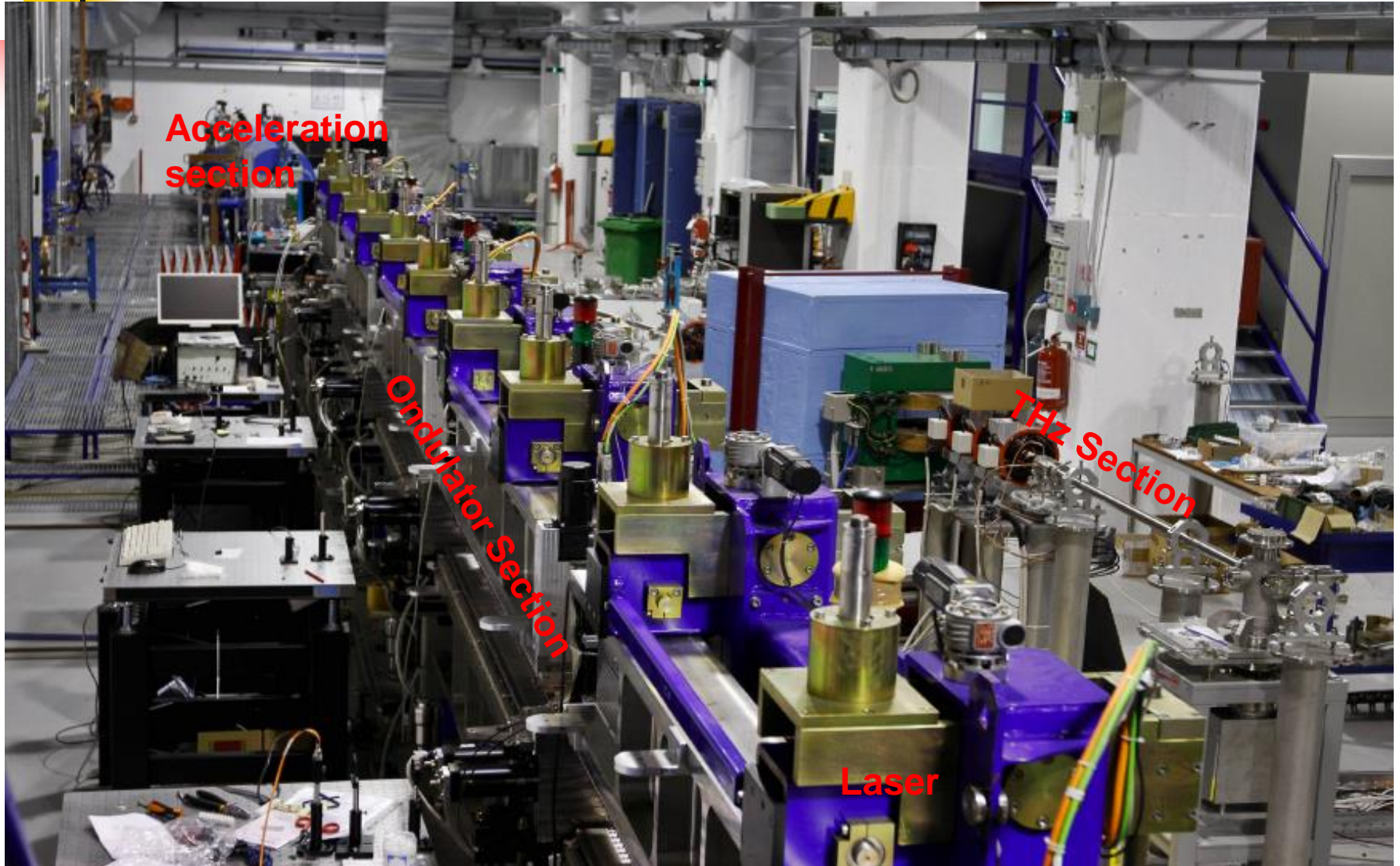
Diffraction Radiation



Undulator Radiation



# SPARC LAB: Linear accelerator at 250 MeV



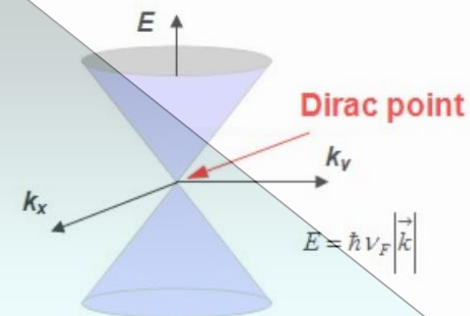
# Achieved THz Performances

Electron beam parameters	Single bunch (VB mode: max compression)	4-bunches per train (VB mode + laser comb)
Charge/bunch (pC)	300	50
Energy (MeV)	130	100
Bunch length (fs)	160	200
Rep. Rate (Hz)	10	

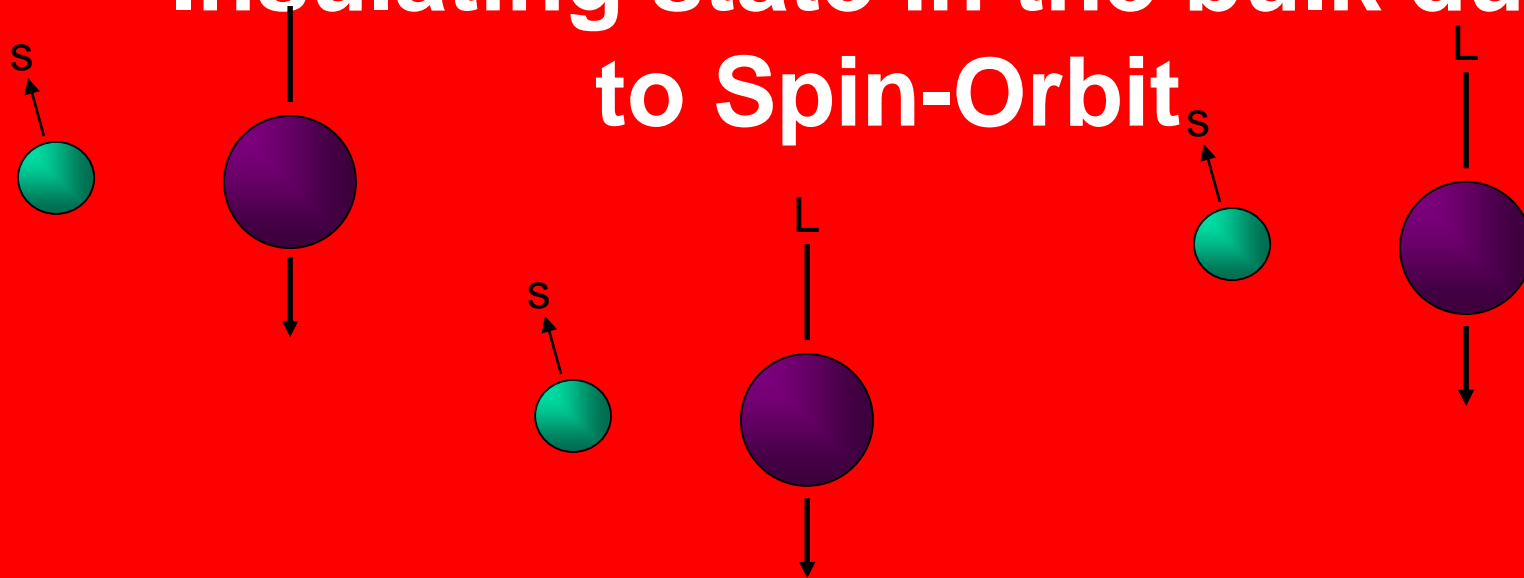
Radiation parameters	SPARC (single bunch)	SPARC (4-bunches/train)
Energy per pulse ( $\mu\text{J}$ )	40	$0.6 \cdot 10^{-6}$ (@ 1 THz)
Peak power (MW)	> 100	3 (@ 1 THz)
Electric field (MV/cm)	1.5	> 10
Pulse duration (fs)	120	< 100
Bandwidth	50 GHz-5 THz	50 GHz-5 THz

# 3D Topological Insulators

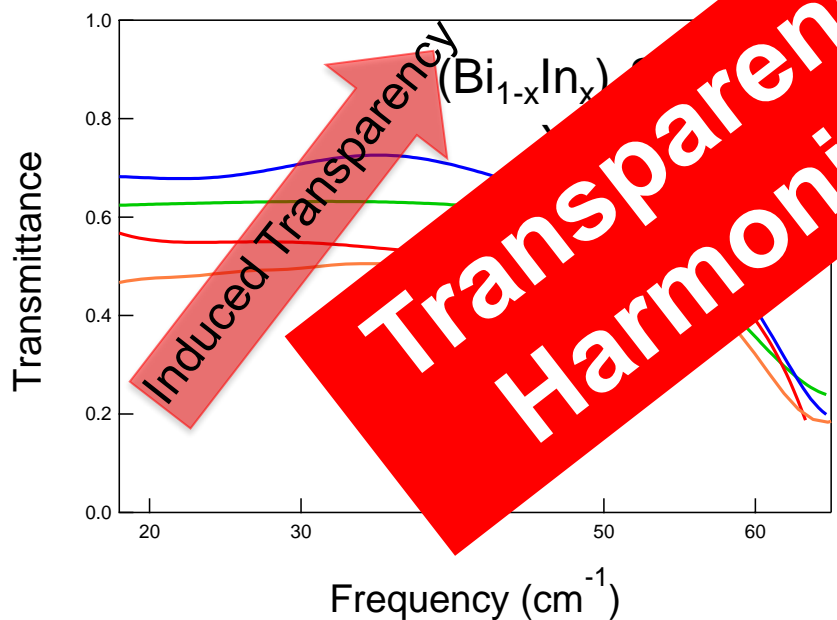
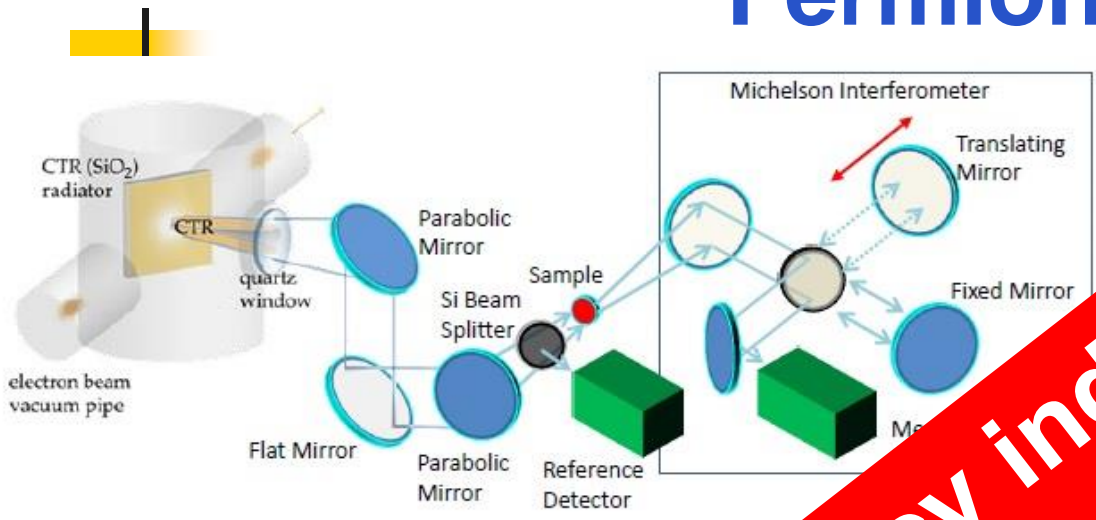
Dirac Metallic Surface



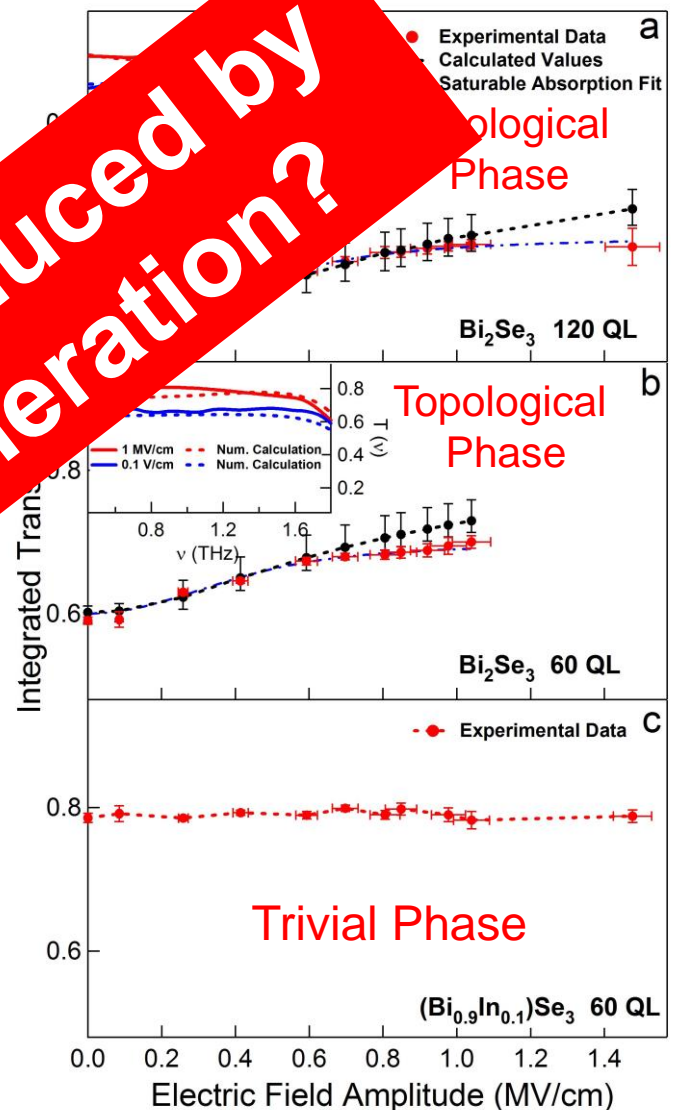
Insulating state in the bulk due to Spin-Orbit



# Non-Linear THz response of TI Dirac Fermions



Transparency induced by Harmonic Generation?





# Non-Linear THz response of TI Dirac carriers

According to the classical equation of motion one electron in an electric field  $\mathbf{E}$  is accelerated with a momentum variation  $d\mathbf{p}/dt = -e\mathbf{E}$ .  $\mathbf{E} = \mathbf{E}_0 \cos \omega t \rightarrow \mathbf{p} = (-e\mathbf{E}_0/\omega) \sin \omega t$

## Massive Electrons

$$\varepsilon(p) = \frac{\vec{p}^2}{2m}$$

$$v_x = \frac{d\varepsilon}{dp_x} = \frac{p_x}{m} = \frac{-eE_0}{m\omega} \sin \omega t$$

For  $n$  electrons one has an electric current

$$J_x(t) = -env_x = \frac{ne^2 E_0}{m\omega} \sin \omega t$$

**Linear current vs.  $\mathbf{E}$**

## Dirac Electrons

$$\varepsilon(p) = v_F \sqrt{p_x^2 + p_y^2}$$

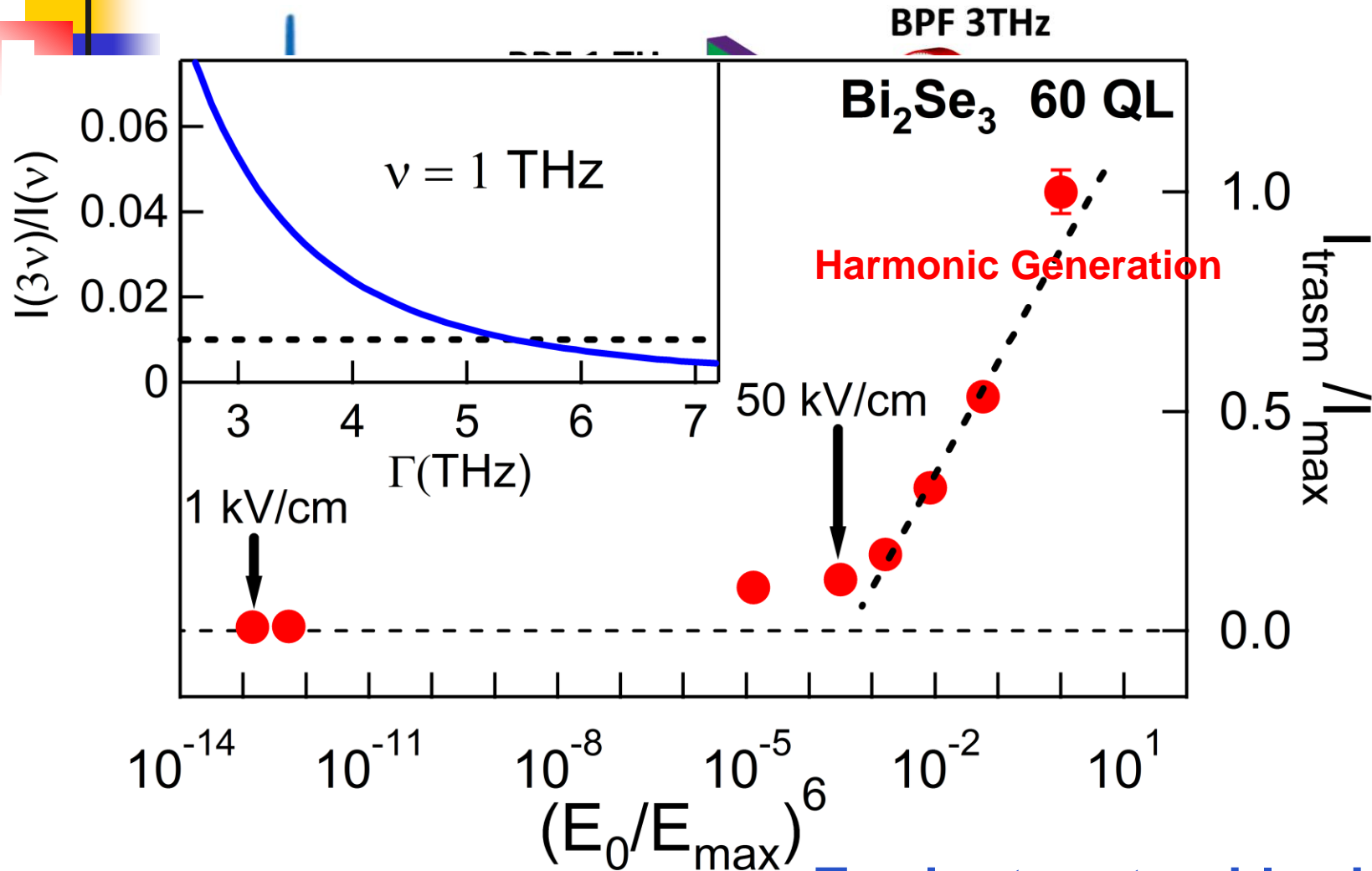
$$v_x = \frac{d\varepsilon}{dp_x} = \frac{v_F p_x}{\sqrt{p_x^2 + p_y^2}} = -v_F \operatorname{sgn} \omega t$$

For  $n$  electrons one has an electric current

$$\begin{aligned} J_x(t) &= -env_x(t) \\ &= e^2 n v_F \frac{4}{\pi} \left[ \sin \omega t + \frac{1}{3} \sin 3\omega t + \dots \right] \end{aligned}$$

**Unlinear current vs.  $\mathbf{E}$**

# Dirac THz Non-Linearity in $\text{Bi}_2\text{Se}_3$ Topological Insulator



**Terahertz saturable absorber**

Freq (THz)

# Go beyond the Diffraction Limit → IRSR Nanoscopy

The resolving capability of an optical component is ultimately limited by the diffraction (Abbe's theory, 1873). The minimum resolution ( $\delta$ ) for the optical component are thus limited by its aperture size, and expressed by:

$$\delta = 0.61 \frac{\lambda}{NA} \approx \lambda$$

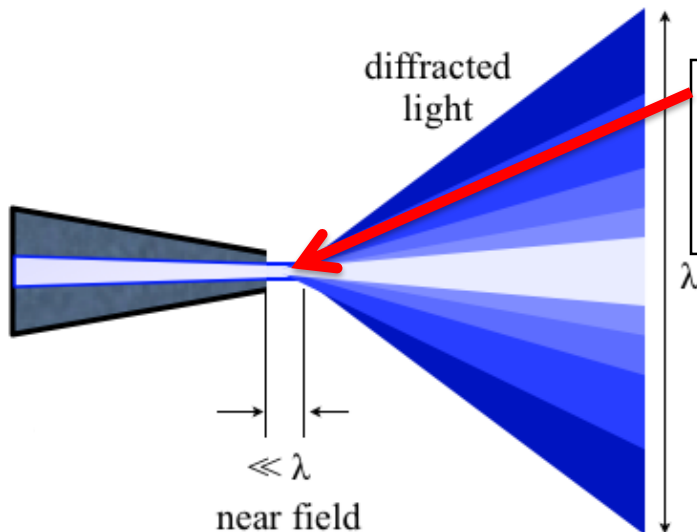
With a 36x objective with NA=0.5, one obtains:

at  $\lambda = 10 \mu\text{m}$  ( $1000 \text{ cm}^{-1}$ ):  $12 \mu\text{m}$

DIFFRACTION

LIMIT

at  $\lambda = 2.5 \mu\text{m}$  ( $4000 \text{ cm}^{-1}$ ):  $3 \mu\text{m}$



The fine spatial structure is contained in the near-field which exponentially decreases far from the focal point

Need to capture the near-field signal



# Beyond the Diffraction Limit: The use of Evanescent waves

In order to enhance the spatial resolution one should increase the wavevector ( $k_x$ ) bandwidth  $\Delta k_x$ :

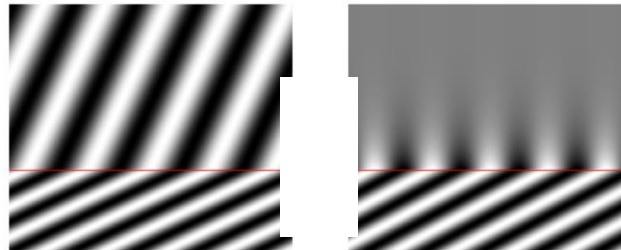
**For propagating light the ultimate limit of  $k_x = k = 2\pi/\lambda$**

Being  $k = \sqrt{k_x^2 + k_y^2 + k_z^2}$ ,  $k_x \gg k = 2\pi/\lambda$  if  $k_z$  is imaginary

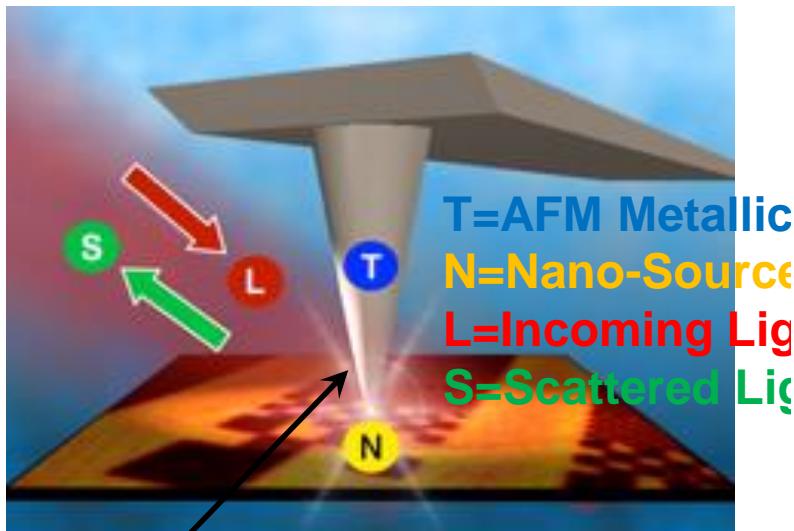
An evanescent wave (along a direction) has along this direction an exponentially decreasing amplitude:

$$E(\mathbf{r}, t) = E_0 e^{ik_x x} e^{ik_y y} e^{-k_z z}$$

Due to the evanescent nature, this wave which maximizes the spatial resolution should be analyzed at distances on the order of  $k_z^{-1} \approx \lambda$  from the source



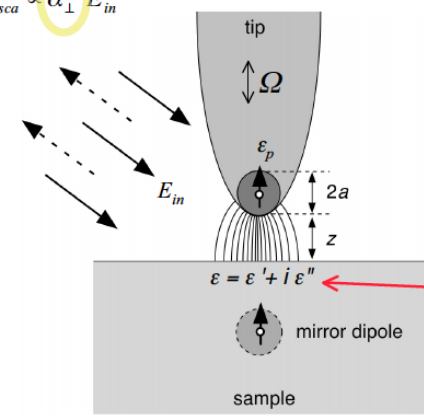
# Generating and Capturing the Evanescent Waves



The metallic AFM-Tip acts as an antenna transforming far-field light into a plasmon which propagates to the apex localizing *em* energy on nanoscale dimension comparable to apex-size.

measured far-field:

$$E_{sca} \propto \alpha_{\perp}^{eff} E_{in}$$



polarizability of tip dipole:

$$\alpha = 4\pi a^3 \frac{(\epsilon_p - 1)}{(\epsilon_p + 2)}$$

effective polarizability of tip and sample:

$$\alpha_{\perp}^{eff} = \frac{\alpha(1 + \beta)}{1 - \frac{\alpha\beta}{16\pi(z+a)^3}}$$

with  $\beta = \frac{(\epsilon - 1)}{(\epsilon + 1)}$

complex  $\epsilon$  determines scattering amplitude and phase

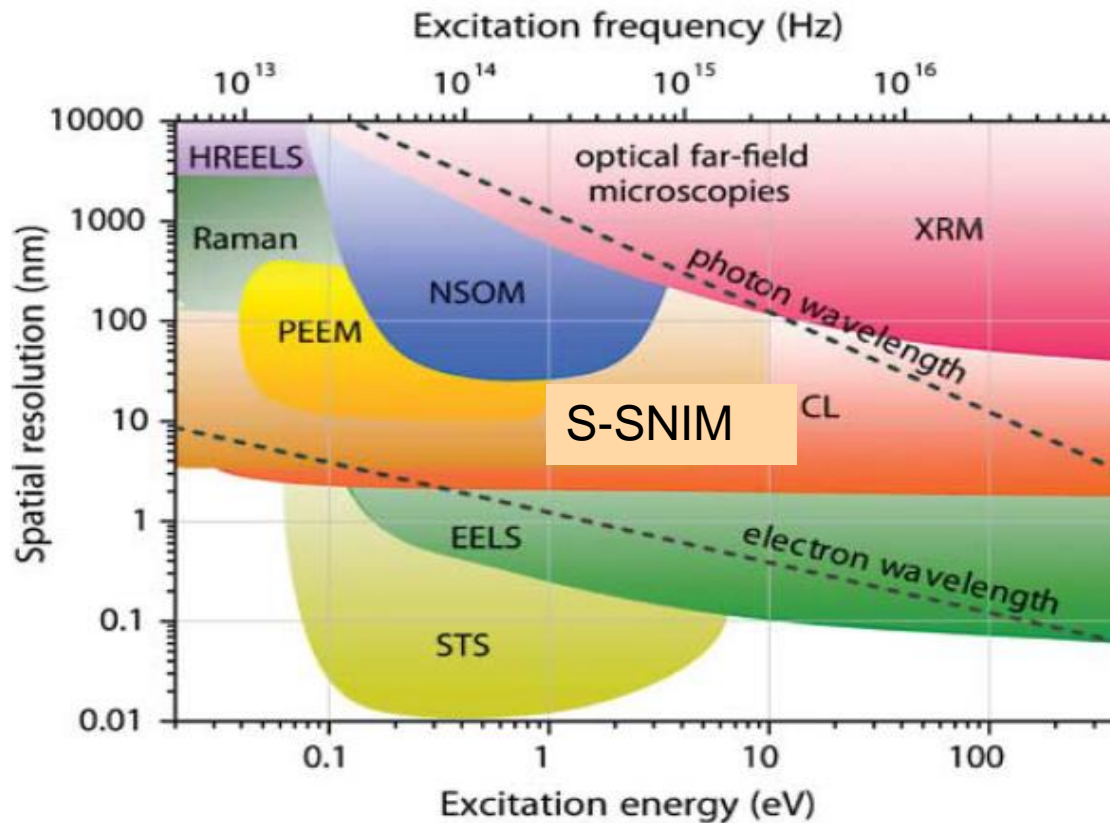
B. Knoll and F. Keilmann, Nature **399**, 134 (1999)

Spatial resolution ~ AFM tip radius



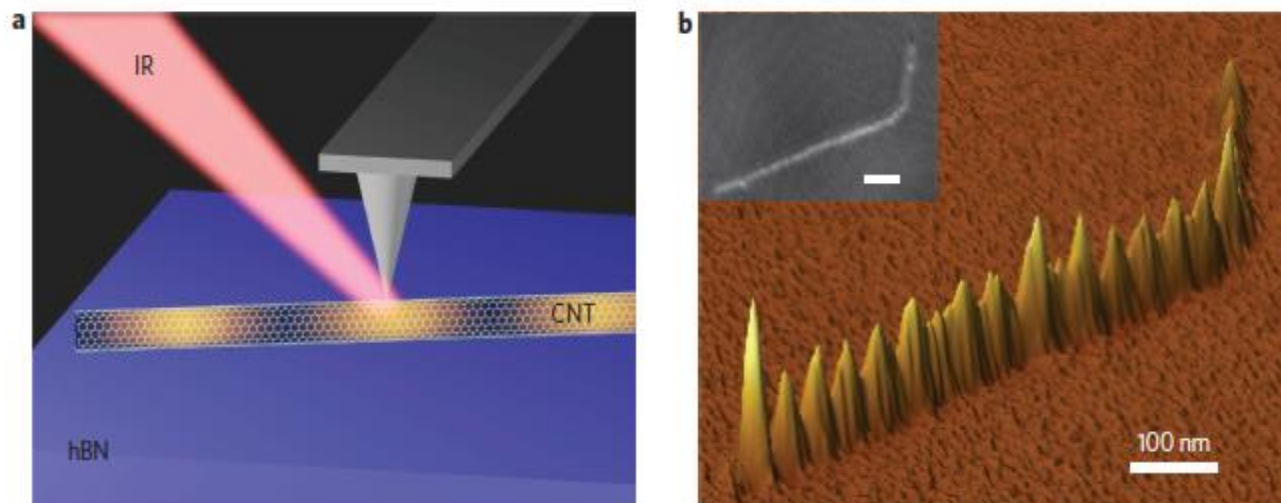
SPATIAL RESOLUTION INDEPENDENT OF  $\lambda$

# Comparison among different Spatially Resolved Spectroscopies



X. F. De Abajo 2010

# Visualizing Plasmon Propagation and Scattering in Single Carbon Nanotube (Optics at Finite $q$ )



**Figure 1 | Infrared s-SNOM of one-dimensional plasmons in carbon nanotubes.** **a**, Illustration of s-SNOM. Infrared (IR) light is focused onto the apex of a metal-coated AFM tip, the large near-field momentum of which enables optical excitation of plasmons in the carbon nanotube (CNT) on a hBN substrate. Interference between the tip-excited plasmon wave and its reflection from the nanotube end leads to periodic modulation of tip-scattered infrared radiation measured by an HgCdTe detector in the far field. **b**, Three-dimensional plot of the near-field scattering intensity (height) along a representative SWNT. Prominent modulation of the infrared scattering intensity from the one-dimensional plasmon can be observed over the whole nanotube. Inset: AFM topography image of the same SWNT. Scale bars, 100 nm.

Z. Shi, Nature Photonics 2015, **IRSR from ALS IR Beamline**

# Acknowledgments

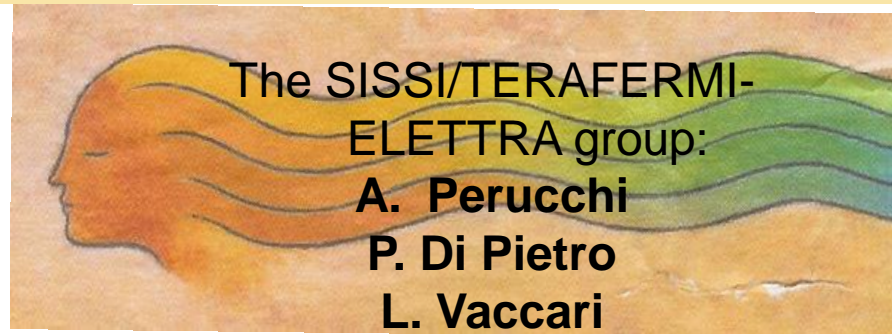


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FREQUENCY AND TIME-RESOLVED  
TERAHERTZ SPECTROSCOPY



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**L. Vaccari**



The LNF-INFN SPARC Lab group:

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